




# A Data-Driven Framework for Power System Event Type Identification via Safe Semi-Supervised Techniques

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**Abstract**—This paper investigates the use of phasor measurement unit (PMU) data with deep learning techniques to construct real-time event identification models for transmission networks. Increasing penetration of distributed energy resources represents a great opportunity to achieve decarbonization, as well as challenges in systematic situational awareness. When high-resolution PMU data and sufficient manually recorded event labels are available, the power event identification problem is defined as a statistical classification problem that can be solved by numerous cutting-edge classifiers. However, in real grids, collecting tremendous high-quality event labels is quite expensive. Utilities frequently have a large number of event records without in-depth details (i.e., unlabeled events). To bridge this gap, we propose a novel semi-supervised learning-based method to improve the performance of event classifiers trained with a limited number of labeled events by exploiting the information from massive unlabeled events. In other words, compared to existing data-driven methods, our method requires only a small portion of labeled data to achieve a similar level of accuracy. Meanwhile, this work discusses and addresses the performance degradation caused by class distribution mismatch between the training set and the real applications. Specifically, this method utilizes pseudo-labeling technique to investigate the value of unlabeled events and incrementally expands the training dataset. Moreover, a safe learning mechanism is developed to mitigate the impacts of class distribution mismatch and prevent performance degradation. Based on the proposed safe learning mechanism, our model does not directly use all unlabeled events during model training, but selectively uses them through a comprehensive evaluation procedure. Numerical studies on a sizable PMU dataset have been used to validate the performance of the proposed method.

**Index Terms**—Event identification, phasor measurement unit, safe learning, semi-supervised model, unlabeled event.

## NOMENCLATURE

CNN Convolutional neural network.  
FP False positive.

FN	False negative.	41
MCC	Matthews correlation coefficient.	42
PMU	Phasor measurement unit.	43
TP	True positive.	44
TN	True negative.	45
$d$	Length of analysis window.	46
$D_l$	New labeled data in each iteration.	47
$f(\cdot)$	Rectified linear function.	48
$h(\cdot)$	Encoder network.	49
$K_l^m$	Kernel filter of the $m$ -th feature map of the $l$ -th layer.	50
$k$	Number of unlabeled events.	52
$L(\cdot)$	Softmax cross-entropy loss.	53
$m$	Number of labeled events.	54
$n$	Size of events.	55
$N_l$	Labeled event set.	56
$N_u$	Unlabeled event set.	57
$N^t$	Number of events marked in the $t$ iteration.	58
$P_l$	Size of feature maps in the $l$ -th layer.	59
$S_f$	Shared feature extractor.	60
$S_1, S_2, S_3$	Three event classifiers.	61
$u$	Classification noise rate.	62
$U^t$	Upper bound of the classification error rate.	63
$W$	Number of repeated estimations in each iteration.	64
$w(\cdot)$	Weight function.	65
$x_i$	PMU measurement for event $i$	66
$y_i$	Label for event $i$	67
$z_i$	Samples from the standard normal distribution.	68
$\omega$	Frequency with which a classifier differs from other classifiers.	69
$\gamma$	Parameter of weight function.	71
$\Omega(\cdot)$	Regularization term.	72
$\varepsilon_G$	Gaussian noise.	73
$\theta$	Parameter of classifier.	74
$\eta_\theta$	Learning rate for $\theta$	75
$\eta_\gamma$	Learning rate for $\gamma$	76
$\tau$	Search space in convolution layer.	77
$\epsilon$	Hypothesis worst-case classification error rate.	78

## I. INTRODUCTION

WITH the modernization of power systems, system operators are expected to meet the growing demands of their

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customers while maintaining the reliability of the power supply. Recently, the increasing penetration of phasor measurement units (PMUs)<sup>1</sup> provides a unique opportunity to improve situational awareness of the system [1]. Typically, PMUs are installed into selected substations and interfaced to the grid via instrument transformers to measure frequency, rate of frequency change, voltage, and current phasors based on the united Coordinated Universal Time reference. PMUs are more accurate and faster (i.e., 30-60 samples per cycle) than supervisory control and data acquisition systems with low sampling rates (i.e., 2-4 samples per cycle) [2]. Inspired by these benefits of PMUs, researchers have dedicated great efforts on data-driven methods for real-time system monitoring and protection using PMU data [3]. Compared to conventional model-based event identification methods, data-based approach has the unique advantage of operating independently of the system.

Depending on whether the model requires a large number of recorded event labels, two categories of existing data-driven event classification methods are summarized. Studies in the first category follow a supervised learning fashion to associate PMU measurements with recorded event labels [4], [5], [6], [7], [8], [9], [10], [11], [12], [13], [14]. In [4], a discrete wavelet transform-based deep neural network model was proposed to reduce false disturbance detection and validate true events. In [5], a three-stage framework was proposed for training robust event classifiers to address the data quality issues of PMU measurements. In [6], two well-established supervised learning methods (i.e., k-nearest neighbor and support vector machine (SVM)) were trained and tested on the basis of thousands of simulated events created by GE's PSLF software. In [7], a three-layer deep neural network-based method was designed to identify power system events using data from 187 PMUs and 1,000 real-world events. In [8], an empirical wavelet transform-based random forest method was proposed to assess power system events. The model was trained and tested based on PSS/E simulation. In [9], a one-versus-many extreme learning machine model was developed to perform event diagnosis by combining 3,495 simulated events and 81 real-world events collected from four PMUs located in Western Electricity Coordination Council. [10] introduced a dictionary of row subspaces of different event types and identified an event by comparing the subspace of the obtained PMU data with the dictionary. In [11], an event characterization algorithm was proposed to calculate spectral kurtosis and used it as the input to SVM for event identification. In [12], a threshold-based OR rule was presented to identify events using rank signatures of PMU measurements. In [13], a deep learning-based event classification model was designed to introduce robustness against bad data issues in online applications. In [14], a symbolic aggregation approximation technique was used to compress and convert PMU data features. Ensemble learning and SVM algorithms were utilized to perform event classification. These efforts have generally shown good results. However, the main concern with category I models is that

good performance depends on the availability of sizable labeled events (e.g., thousands of simulated events). As demonstrated concretely in [15], limited training samples usually reduce the accuracy and generalization of supervised event classification models. In reality, even for stable grids with long-term operations and few events, the number of event labels is limited.

Utilities often have records of events without in-depth details. Of the 2,226 recorded events observed by Public Service Company of New Mexico over four years, only 97 events were registered in the event logs [16]. Considering that category I methods typically struggle to perform adequately with few labeled events, researchers are exploring a variety of unsupervised and transfer learning strategies to perform event detection and identification [17], [18], [19], [20], [21], [22], [23]. In [17], a heterogeneous joint domain adaptation method with a transfer learning strategy was proposed to transfer knowledge from a data-rich source grid to the data-limited target grid to boost the machine learning performance in the target grid. In [18], a statistics-based framework was proposed to detect events using PMU data. In [19], a two-stage framework was proposed to achieve real-time event detection, physically meaningful event type distinction, and localization using principal component analysis and hierarchical clustering technique. In [20], a transfer learning-based mechanism was proposed to address the issue of event detection from a remarkably small number of labeled events. In [21], three existing clustering algorithms (i.e., partitioning, hierarchical, and density-based methods) were evaluated to group disturbance files. In [22], a novel characteristic ellipsoid method was proposed to identify types and locations of transient events. In [23], a kernelized tensor decomposition and classification framework was proposed to incorporate rich unlabeled data. While existing unsupervised and transfer learning-based event identification works provide valuable results, several questions remain open. For example, unsupervised learning-based methods cannot provide the physical meaning of event types. The results of these methods are usually broadly defined categories and thus can only provide limited help for real-time system monitoring. A natural way to deal with this question is to associate and define each category using data from labeled events and domain knowledge. However, this solution relies on an important assumption that labeled events and unlabeled event types are identical. In other words, the utilities need to observe and register all possible event types. In practice, it is difficult to maintain such an assumption. Unlabeled events often hide a variety of new event types, which is also mentioned by previous work [6]. In this paper, this situation is referred to as the *class distribution mismatch problem* (as shown in Fig. 1), which greatly increases the difficulty of data-driven event classification tasks. Last but not least, the results of unsupervised techniques tend to have low accuracy due to the lack of labeling information.

To address these problems, this paper proposes a novel data-driven model to identify power event types in a semi-supervised learning manner. Compared to supervised learning-based models, the proposed model is better suited for real-world tasks because collecting tremendous high-quality event labels is quite expensive. To achieve this, our method leverages an output smearing strategy to build three different classifiers and initially

<sup>1</sup>According to statistical data provided by the North American SynchroPhasor Initiative, over 1,900 PMUs have been installed in the U.S., which is a nine-fold growth from 2009.

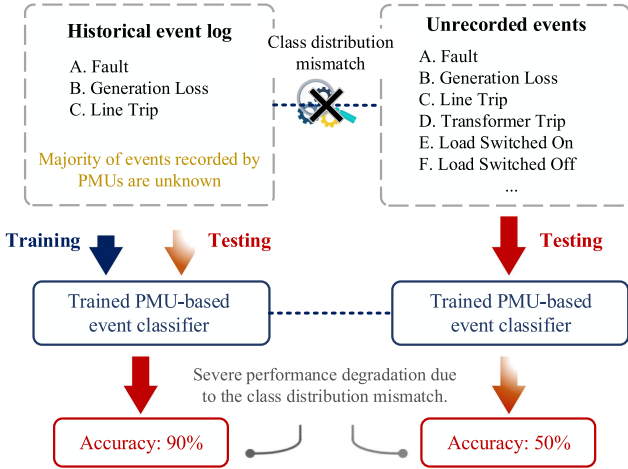


Fig. 1. Description of the event identification problem under the class mismatch problem.

trains them using labeled events in parallel. Considering the high model complexity due to the high dimensionality of PMU measurements, convolutional neural networks (CNNs) are used as the underlying classifier in this work. The unique benefit of utilizing three event identifiers is that it provides a workaround for marking unlabeled events. Specifically, if any two of classifiers have a consistent estimate for an unlabeled event, then this estimate is confident and can be added to the training set. The three event identifiers are retrained using the updated training set in order to consistently benefit from the abundance of unlabeled events. Considering that unseen event types do not exist in the initial training set, it is impossible for three classifiers to give meaningful estimates for these types. Therefore, the training process of each model is projected as a bi-level optimization problem to avoid pseudo-labeling of events under unseen types as much as possible, which is defined as a safe learning mechanism. A weighted empirical risk minimization model is to be obtained in the inner-layer optimization. Additionally, the goal of the outer-layer optimization is to minimize classification loss on a given training set. An online approximation method is applied to solve this bi-level optimization. By combining these novel modules, a better generalization ability can be achieved. The main contributions of this paper can be summarized as follows:

- The proposed framework can improve the performance of event classifiers trained with a limited number of labeled events. The proposed method is able to achieve similar accuracy as supervised learning methods using all labeled data, but using only 25% of the labeled data.
- The proposed framework not only exploits the value of unlabeled events, but also provides a basis for significantly reducing the impact of the class distribution mismatch problem to enhance event classifier performance.
- The proposed safe learning strategy prevents features of unseen events from becoming entangled with features of observed events, thus avoiding performance degradation of the model on known event types. Such a mechanism

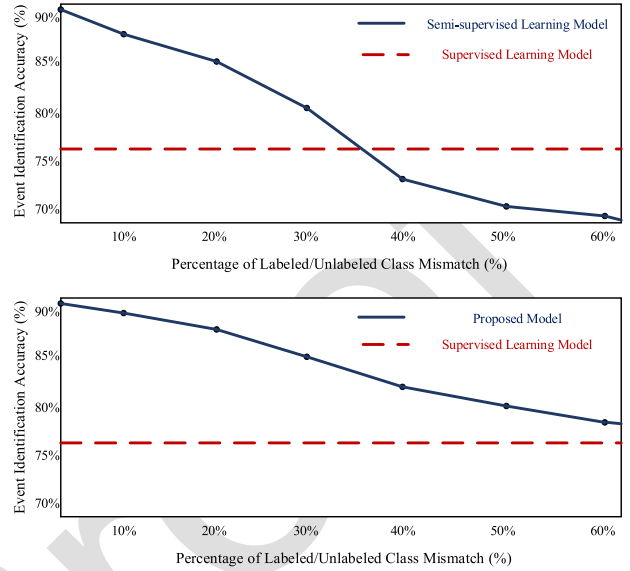


Fig. 2. As the class distribution mismatch ratio between the labeled and unlabeled data rises, the performance of traditional semi-supervised learning approaches drastically declines. When the mismatch exceeds a certain range, the performance of the traditional semi-supervised learning method is even worse than that of the supervised learning method (top). Such a performance degradation hinders the motivation to use semi-supervised learning techniques in the vast majority of real applications. In contrast, the performance of the proposed method similarly declines as the class distribution mismatch between labeled and unlabeled data increases, but it never performs worse than the performance of the supervised learning method (bottom).

can help the proposed model to perform no worse than its supervised counterpart in extreme cases.

- The proposed model was developed and tested based on two years of data from hundreds of PMUs and approximately 4,800 event records from Western Interconnection. In our experiments, we constantly assume that a portion of the event records are unknown to simulate different real situations. All results are derived by comparing predictions and ground truths.

The rest of this paper is structured as follows. The preliminaries of the proposed framework are shown in Section II, including the data description and problem formulation. Section III introduces the semi-supervised learning-based event identification. Section IV presents the safe learning process. Case studies are demonstrated in Section V. Research conclusions are provided in Section VI.

## II. PRELIMINARIES

### A. Data Description and Pre-Processing

The available 2-year PMU measurements were initially collected by regional system operators and utilities in the Texas, Western, and Eastern Interconnections of the U.S. and then formatted by Pacific Northwest National Laboratory. Each PMU monitors the system frequency, voltage, and current phasors, as well as the rate at which the frequency changes. The majority of PMU data segments are archived at 30 frames per second and the rest at 60 frames per second. In addition to 20 TB of

PMU streaming data, this dataset has the particular advantage of containing enough real event labels (i.e., 6,767 events from utilities), which creates a solid foundation for designing an effective event classification model. Note that complete detection criteria for all types of events and historical protection records are not provided in this work due to the safeguarding of sensitive information, making them unavailable for classification model development.

The data pre-processing is done prior to model development to assure the quality of the training data, preventing inaccurate event detection brought on by data quality issues. This procedure is empirical and follows the guidance of our industrial partners. Briefly, the first phase in data pre-processing is to use PMU status flag information to identify data with data quality issues. According to IEEE C37.118.2-2011 standard, when the decimal status flag value is 0, PMU measurements can be used to accurately describe the system status. Instead, PMU is in a malfunction state. In addition, based on engineering intuition, we designed several threshold-based methods to identify data quality issues that are not detected by the PMU itself, such as out-of-range issues. In the second phase, when consecutive missing or bad data happens, the data is removed from our study. The justification for this is that it is challenging to offer precise data imputation for these consecutive bad data, which is also out-of-scope of this work. Linear interpolation is then used to fill in and repair the remaining missing or bad data. After data processing, the latent data features are extracted using Markov transition field techniques. By calculating Markov transition probabilities and converting that data into graphs, Markov transition fields can preserve all time-domain information. More details can be found in our previous works [13], [24]. Note that the system topology, PMU locations, and historical event locations are not available. Hence, this work cannot be extended to identify the location of events. We leave it for future work. Once they are available, more comprehensive results will be provided.

## B. Problem Formulation

In terms of notation, let  $x_i$  denote its  $i$ -th entry in a column vector  $\mathbf{x}$ . Given a matrix  $\mathbf{X}$ , let  $X_{(i,j)}$  denote its entry at  $i$ -th row and  $j$ -th column and  $[\mathbf{X}]_i$  denotes its  $i$ -th row. The estimation is indicated by the superscript  $(\hat{\bullet})$  and the optimum is shown by the superscript  $(\bullet)^*$ .

Consider a set of PMU data  $N_l = \{(x_1, y_1), \dots, (x_m, y_m)\}$ , the data-driven event identification problem can be formulated as an  $n$  type classification problem [7], where  $x_i \in \mathbb{R}^{d \times 1}$  is the measurement data of PMU with  $d$ -length analysis window<sup>2</sup>,  $y_i \in \{1, \dots, n\}$  is the label recorded in the disturbance files after using a label encoding technique,  $m$  is the total number of recorded events, and  $n$  is the number of event types. In order to achieve satisfactory event identification accuracy, a

large amount of labeled events are necessary.<sup>3</sup> However, in power systems, such a condition is difficult to meet because obtaining labeled events is costly in terms of human and financial resources. As mentioned in previous work [6], most of the events recorded by PMUs are unknown. Therefore, the event identification problem needs to be refined to an  $n+1$  type classification problem, where  $N_l = \{(x_1, y_1), \dots, (x_m, y_m)\}$  and  $k$  unlabeled events  $N_u = \{x_{m+1}, \dots, x_{m+k}\}$ . Here,  $y_i \in \{1, \dots, n+1\}$ , where  $(n+1)^{\text{th}}$  represents an unspecified type recorded in event logs. For the  $(n+1)^{\text{th}}$  type, a natural assumption is that the  $(n+1)^{\text{th}}$  type is a mixture of known event types. This is one of the common assumptions used in previous works [17], [19], [20], [22]. Under this assumption, the lack of labeled event data can be overcome by finding associations between known event types and the  $(n+1)^{\text{th}}$  type using state-of-the-art unsupervised techniques. However, this assumption is not practical in many cases. In reality, the number of unlabeled data is much larger than the number of labeled data (i.e.,  $k \gg 0$ ). This results in the  $(n+1)^{\text{th}}$  type often consisting of two parts: the events belonging to the known types but not identified by utilities and all other types of events that are not seen in the event logs. Hence, unrecorded events and recorded events do not share the same distribution, which is known as class distribution mismatch, as shown in Fig. 1. Note that our model is built based on this actual situation rather than on the previous assumption. When the different unknown events that are classified in the  $(n+1)^{\text{th}}$  type have markedly different underlying physics, they may have highly distinct characteristics and cannot be categorized in any of the known types. Face with this situation, since conventional semi-supervised models have never seen the types of these events, it is impossible for the model to provide correct estimation for unlabeled set and derive any useful information from them. Moreover, the characteristics of the unknown events are entangled with the characteristics of the observed events, which significantly impairs the trained model's ability to judge events of known types (also known as performance degradation). This is the reason why most semi-supervised learning algorithms no longer work well, and may even be worse than a simple supervised learning model (i.e., support vector machine, logistic regression, and random forest) [25]. It should be noted that supervised models do not suffer from this problem, as they only focus on those labeled events. Such shortcomings limit the application of deep semi-supervised models in power event classification problems.

To develop a practical event identification model, we propose a safe tri-net-based method that only requires limited labeled events without any class distribution assumptions. Briefly, our work uses the idea of pseudo labeling to discover the value of unlabeled events<sup>4</sup> to improve the performance of the event

<sup>2</sup>In this work, a 2-second analysis window is utilized to intercept PMU measurements based on event logs. This 2-second analysis window consists of 0.5 pre-event data and 1.5 post-event data. The value of  $d$  is determined based on previous studies [13], [24]. Note that the selection of  $d$  is a trade-off between event information and the curse of dimensionality. Also, as the input dimension increases, the computation complexity of the data-driven event identification model grows significantly, which can impact the real-time application of models.

<sup>3</sup>The amount of data required for machine learning depends on many factors, including the complexity of the problem and the complexity of the learning algorithm. Based on the high sampling rate of PMUs, the amount of data required to realistically train and test a classifier is enormous.

<sup>4</sup>Pseudo labeling is a commonly-used method to perform semi-supervised learning tasks. The basic idea of this method is to seek the generation of pseudo labels for unlabeled samples to guide the learning process in an alternating manner. Specifically, the initial model is trained using the limited labeled data.

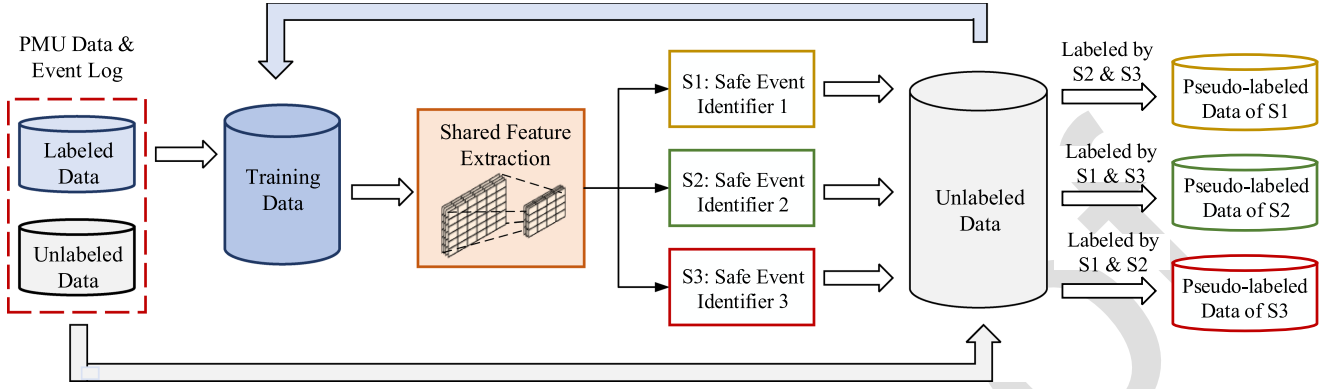


Fig. 3. Overall framework of the proposed safe learning-based event identification model.

identifiers when training with limited event logs [26]. However, unlike previous models, our method can handle class distribution mismatch by incorporating a bi-level optimization in the backpropagation process. By designing a weight function, the proposed method uses unlabeled data selectively. In each iteration, the model searches for the optimal model parameters based on weighted empirical risk minimization. The weight function parameters are then improved to continuously track the supervised performance once the obtained model parameters are evaluated on labeled events. The trained event identifier will therefore not perform worse than a supervised learning-based event identification model when utilizing our method, even if event logs do not cover all event types. We will demonstrate in the following section that the event identifier learned using the proposed approach is always better than the model developed using simply labeled data.

### C. Proposed Event Identification Framework

The objective of this work is to design a framework to improve the performance of event classifiers in a safe manner. Given the prevalence of unlabeled data in all grids, the data resources required to train the proposed event classification model consist of unlabeled data and a limited amount of labeled data. Different stages of the proposed framework are demonstrated in Fig. 3.

- *Stage I - Tri-net Classifier Initialization:* A tri-net-based framework is developed to perform event identification in a semi-supervised learning manner. As shown in Fig. 3, the proposed framework consists of a shared feature extractor ( $S_f$ ) and three safe event identification modules ( $S_1$ ,  $S_2$ , and  $S_3$ ) with different structures. The three event classifiers build the mapping relationship between shared features and event types. An output smearing strategy is used to construct three diverse training sets, thus augmenting diversity between three classifiers (detailed in Section III).
- *Stage II - Safe Learning-based Parameter Optimization:* A safe learning mechanism is proposed to update model parameters for each classifier. Such a mechanism can prevent performance degradation due to the class distribution

mismatch problem. The basic idea is to weaken unlabeled data with unseen classes by adding a weight function and tracking supervised loss by designing a bi-level optimization (detailed in Section IV).

- *Stage III - Pseudo-Label Dropout:* To further deal with the low-confidence pseudo labels, a dropout strategy is applied during the training process. Basically, this strategy exploits the disagreements among the three classifiers. With three classifiers, if any two of them have a consistent estimate for an unlabeled event, then this estimate is confident and can be added to the training set, as shown in Fig. 3. Such an augmented training set is utilized to refine the three classifiers until the end of the training process (detailed in Section IV).

## III. SEMI-SUPERVISED LEARNING-BASED EVENT IDENTIFICATION

This section outlines the proposed safe tri-net-based approach. We quickly review the concepts and characteristics of conventional semi-supervised learning techniques before describing our method in depth to help the reader comprehend the proposed model.

Semi-supervised learning is a learning paradigm linked with developing models using all available data, including labeled and unlabeled data, and is conceptually positioned between supervised and unsupervised learning. Compared to supervised learning approaches, Semi-supervised learning techniques are better suited for real-world tasks where unlabeled data are easily accessible whereas labeled cases need more resources and time to collect. The goal of the semi-supervised learning model is to use all available data to generate a predictive function that is more accurate than the one obtained using only labeled data. When dealing with classification problems, leveraging unlabeled data with a semi-supervised method can provide us with additional information about the shape of the decision boundary among different classes. According to previous studies, semi-supervised learning methods can be broadly divided into two categories: transductive learning and inductive learning [27]. Basically, transductive learning aims to apply the trained models to the unlabeled data observed at training time; in this case, it

Then, the trained model is utilized to generate pseudo labels for the unlabeled samples. Based on the updated training dataset, the model is retrained.

429 does not generalize to unobserved data. In contrast, the goal of  
430 inductive learning is to learn a model capable of generalizing to  
431 unobserved data at test time. This categorization applies to the  
432 proposed approach.

433 One of the major challenges of the semi-supervised event  
434 identification method is how to produce additional training  
435 data by labeling instances of the unlabeled set. Inspired by  
436 the tri-training methodology [26], the proposed model utilizes  
437 three different classifiers to handle the challenge of identifying  
438 unlabeled events. It should be noted that the initial classifiers  
439 should be diverse. When all classifiers are the same, they will  
440 all produce the same estimate for each unlabeled event, which  
441 will impede the model training. In this work, to construct three  
442 diverse modules, an output smearing strategy is applied [28]. By  
443 adding random noise to true labels, this strategy can construct  
444 diverse training sets, which can be formulated as follows:

$$\hat{y}_i = y_i + f(z_i \times \sigma_i) \quad (1)$$

445 where,  $z_i$  is sampled independently from the standard normal  
446 distribution,  $\sigma_i$  is the standard deviation, and  $f(\cdot)$  is represented  
447 by the rectified linear function. With the output smearing strat-  
448 egy, three diverse training sets can be obtained from the initial  
449 labeled set. Then, the objective function of our method is to  
450 minimize the sum of the three identifiers' losses, which is defined  
451 as follows:

$$\min_{\Theta} \sum_{i=1}^m \{L(S_1(S(x_i), \hat{y}_i^1)) + L(S_2(S(x_i), \hat{y}_i^2)) + L(S_3(S(x_i), \hat{y}_i^3))\} \quad (2)$$

452 where,  $L(\cdot)$  denotes the standard softmax cross-entropy loss in  
453 this work (i.e., a softmax activation plus a Cross-Entropy loss).  
454 The shared module  $S_f$  is designed by using one convolutional  
455 and max-pooling layers. The parameters of the  $S_f$  are updated  
456 by learning all gradients from  $S_1$ ,  $S_2$ , and  $S_3$ . The structure  
457 of classifiers  $S_1$ ,  $S_2$ , and  $S_3$  are derived from state-of-the-art  
458 convolutional neural network architecture [29]. To get more  
459 diversity among the three classifiers, different structures (i.e.,  
460 different network depths and convolution parameters) were used  
461 for the three classifiers. In order to assist readers unfamiliar with  
462 deep learning, we outline each typical layer below:

463 • *Convolutional Layer*: Convolutional layers typically run  
464 an operation ( $*$ ) on the input and pass the result to the  
465 following layer. In this work, after feature reconstruction,  
466 all event signals are considered as two-dimensional graphs,  
467 making the convolutional layer mathematically formulated  
468 as follows:

$$\begin{aligned} & (x_{l-1} * K_l^m)(i, j) \\ &= \sum_{\tau_i=0}^{P_l} \sum_{\tau_j=0}^{P_l} x_{l-1}^s(i - \tau_i, j - \tau_j) K_l^m(i, j) \end{aligned} \quad (3)$$

469 where,  $K_l^m$  is the kernel filter of the  $m$ -th feature map of  
470 the  $l$ -th layer,  $P_l$  refers to the size of feature maps in the  $l$ -th  
471 layer, and  $\tau_i$  and  $\tau_j$  are the search paces in the horizontal

472 and vertical directions, respectively. As a result, the con-  
473 volutional layer performs an element-wise multiplication  
474 in a sliding-window manner. It will summarize the results  
475 into a single output and transform a feature matrix into a  
476 different feature matrix, whose dimensionality of the new  
477 matrix is determined by the dimensionality of the original  
478 matrix and the dimensionality of the kernel filter.

- 479 • *Activation Layer*: To compensate for the limitations of  
480 linear modeling in the convolutional layer, the results of  
481 the convolutional layer are given to a nonlinear function  
482 (e.g., sigmoid, tanh, softmax, ReLU, leaky ReLU, etc.).  
483 The activation layer is the name given to this nonlinear  
484 function. In this study, all layers but the fully linked layer  
485 are activated using Leaky-ReLU, while the fully connected  
486 layer is activated using soft-max.
- 487 • *Max-pooling Layer*: The feature maps are aggregated using  
488 a maximum pooling layer following activation function and  
489 batch normalization. Max pooling is essentially a pooling  
490 procedure that chooses the largest element from the feature  
491 map region that the filter covers. In other words, a feature  
492 map comprising the standout features from the prior feature  
493 map will be the output following the maximum pooling  
494 layer. In this paper, a  $2 \times 2$  max-pooling is used.

495 In contrast to conventional semi-supervised models that re-  
496 quire explicitly measuring confidence in pseudo-labeling (i.e.,  
497 self-training), our method provides a natural and efficient mech-  
498 anism for evaluating pseudo labels of unlabeled events. As  
499 demonstrated in Fig. 3, for any identifier, an unlabeled event can  
500 be labeled when two other identifiers agree on the label of this  
501 event. For example,  $x_i$  can be added to the training set for  $S_3$  if  $S_1$   
502 and  $S_2$  concur on the label of the event. Following this strategy,  
503 each classifier is retrained using the augmented training set in  
504 each iteration. Note that the structure of the classifiers should be  
505 different. Otherwise, the unlabeled events identified by the other  
506 two classifiers will be the same as those labeled by the other two  
507 classifiers for either of the classifiers. Obviously, even if our  
508 method uses two classifiers to increase the confidence of pseudo  
509 labels, incorrect pseudo-labeling is inevitable. These incorrect  
510 pseudo labels would degrade the performance of the classifiers  
511 during the training process. Therefore, we will show that the  
512 increase in the classification error can be offset if the amount of  
513 newly labeled data can adhere to certain requirements:

514  $S_1$  and  $S_2$  classified instances with pseudo-labels are added to  
515 the training set of  $S_3$  as examples to prove our conclusion above.  
516 First, let  $N^t$  and  $N^{t-1}$  refer to the number of data that are labeled  
517 for  $S_3$  in the  $t$ -th and  $t - 1$ -th iteration, respectively. Let  $u_{N_l}$   
518 and  $U_{S_1, S_2}^t$  denote the classification noise rate of the original  
519 training set  $N_l$  and the upper bound of the classification error  
520 rate caused by  $S_1$  and  $S_2$  at the  $t - 1$ -th iteration. According to  
521 the finding of [30], the inverse of the square of the error at the  
522  $t$ -th iteration (i.e.,  $\frac{1}{(\epsilon^t)^2}$ ) can be formulated as:

$$\frac{1}{(\epsilon^t)^2} = |N_l \cup N^t| \left( 1 - 2 \frac{(u_{N_l} |N_l| + U_{S_1, S_2}^t |N^t|)}{|N_l \cup N^t|} \right)^2 \quad (4)$$

523 Basically, if  $\epsilon^t < \epsilon^{t-1}$ , it implies that  $S_3$  can be improved  
524 through using newly labeled data (i.e.,  $D_t$ ) from  $S_1$  and  $S_2$ :

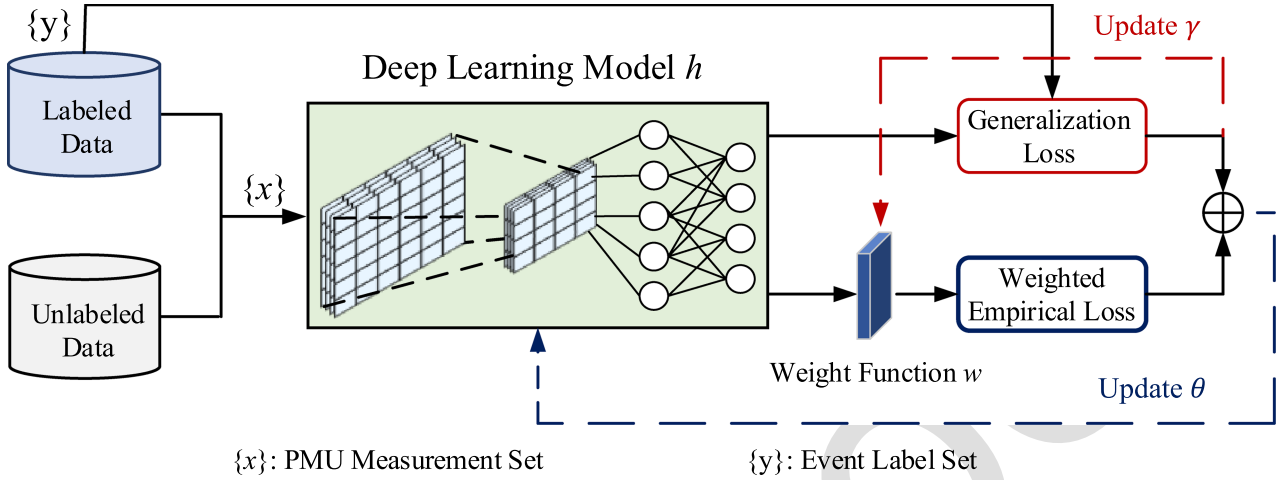


Fig. 4. Illustration of safe event identification model.

525

$$|N_L \cup N^t| \left( 1 - 2 \frac{(u_{N_l} |N_l| + U_{S_1, S_2}^t |N^t|)}{|N_l \cup N^t|} \right)^2 > |N_l \cup N^{t-1}| \left( 1 - 2 \frac{(u_{D_l} |D_l| + U_{S_1, S_2}^{t-1} |N^{t-1}|)}{|D_l \cup N^{t-1}|} \right)^2 \quad (5)$$

526 When  $U_{S_1, S_2}^t$  and  $U_{S_1, S_2}^{t-1} \in [0, 0.5)$ , (5) always holds if  $|N^t| >$   
 527  $|N^{t-1}|$  and  $U_{S_1, S_2}^{t-1} |N^{t-1}| > U_{S_1, S_2}^t |N^t|$ . In sum,  $S_3$  can be  
 528 improved when the following constraint is satisfied:

$$0 < \frac{U_{S_1, S_2}^t}{U_{S_1, S_2}^{t-1}} < \frac{|N^{t-1}|}{|N^t|} < 1 \quad (6)$$

529 This constraint cannot hold when  $|N^t|$  is far bigger than  $|N^{t-1}|$ ,  
 530 which is possible. When this occurs, a subsampling method is  
 531 applied for  $N^t$  randomly remove a portion of the data to maintain  
 532 (6). It is combined with the proposed structure to specify the  
 533 conditions under which unlabeled data may be labeled for a  
 534 classifier.

#### 535 IV. SAFE EVENT IDENTIFICATION MODEL

##### 536 A. Model Formulation

537 Considering that class distribution mismatch occurs in actual  
 538 grids, it is not reasonable to estimate pseudo labels to unlabeled  
 539 data under unseen classes because the training model never  
 540 learns the features of this class. Such a problem leads to severe  
 541 performance degradation when applying conventional semi-  
 542 supervised learning techniques in power event identification.  
 543 To solve this question, a safe learning mechanism is proposed  
 544 based on the structure mentioned in the previous section. Specifi-  
 545 cally, the proposed mechanism designs a weight function to use  
 546 unlabeled data selectively and continuously tracks the performance  
 547 of the supervised learning model to prevent performance  
 548 degradation. To achieve this, each event classifier (i.e.,  $S_1$ ,  $S_2$ ,  
 549 and  $S_3$ ) is destined as a bi-level optimization problem, where  
 550 one optimization problem is nested inside another issue. Fig. 4

describes this process. The basic idea is to use as many beneficial  
 551 unlabeled events as possible and keep track of supervised loss  
 552 to prevent performance degradation. To achieve this, first, our  
 553 method minimizes a weighted empirical risk<sup>5</sup> by integrating a  
 554 weight function with a regularization strategy for the unlabeled  
 555 events. The objective function can be formulated as follows:  
 556

$$\hat{\theta} = \min_{\theta} \sum_{i=1}^m L(S(x_i; \theta), y_i) + \sum_{i=m+1}^{m+k} w(x_i; \gamma) \Omega(x_i; \theta) \quad (7)$$

557 where,  $\hat{\theta}$  is denoted as the model trained with the weight function  
 558 parameterized by  $\gamma$ , and  $\Omega(\cdot)$  refers to the regularization term. In  
 559 this work, we have applied a consistency regularization strategy  
 560 to formulate  $\Omega(\cdot)$  [31]:

$$\Omega(x; \theta) = \|h(x + \varepsilon_G; \theta) - h(x; \theta)\|_2^2 \quad (8)$$

561 where,  $h(\cdot)$  is a standard encoder network that maps input data to  
 562 a lower dimensional space and  $\varepsilon_G$  refers to Gaussian noise. The  
 563 aim of the regularization term is to train a model that is invariant  
 564 to various data augmentations, which provides the basis for using  
 565 unlabeled data to augment prediction function [32].<sup>6</sup> Using the  
 566 weight function, unlabeled events can be utilized selectively,  
 567 thus reducing the impact of the distribution mismatch problem.  
 568 Then, the proposed model evaluates  $\hat{\theta}$  on  $m$  labeled events  
 569 and optimizes the weight function parameter  $\gamma$  to avoid severe  
 570 performance degradation. This optimization can be formulated  
 571 as follows:

$$\hat{\gamma} = \min_{\theta} \sum_{i=1}^m L(S(x_i; \theta), y_i) \quad (9)$$

<sup>5</sup>Empirical risk minimization is a principle in statistical learning theory, which is commonly used to give theoretical bounds on their performance. The basic idea is to measure model performance on a known set of training data rather than an unknown true data distribution.

<sup>6</sup>Mathematically, using pseudo-labeled data to augment the training set first requires adherence to the notion: if an actual perturbation is applied to an unlabeled data, the prediction should not change significantly. The underlying rationale behind this is that data points with different labels should be low density separation based on cluster assumption.

In summary, the first optimization of the proposed safe event identification (7) is to seek the optimal model parameters  $\hat{\theta}$  using the entire dataset. For convenience, let  $A(\theta, \gamma)$  denotes as (7). Next, the learned model parameter  $\hat{\theta}$  is evaluated in the labeled dataset and the weight function parameters  $\gamma$  are optimized, as shown in (9), to achieve a better reliable performance, which is represented by  $B(\theta)$ . Consequently, the following bi-level optimization problem can be expressed as the objective of the proposed safe event identification model:

$$\min_{\gamma} \sum_{i=1}^m L(S(x_i; \hat{\theta}), y_i) \quad (10)$$

$$s.t. \hat{\theta} = \min_{\theta} \sum_{i=1}^m L(S(x_i; \theta), y_i) + \sum_{i=m+1}^{m+k} w(x_i; \gamma) \Omega(x_i; \theta) \quad (11)$$

The unique benefit of the proposed safe learning mechanism is to introduce safeness in terms of empirical error. In other words, by optimizing  $\gamma$ , the proposed method does not perform worse than its supervised counterpart.

### B. Model Training

Since there is no closed-form expression for this bi-level optimization problem, it necessitates two nested loops of optimization to obtain the optimal  $\gamma^*$ .<sup>7</sup> As a result, the computational complexity of the training process increases significantly as the size of the training data increases. To address this issue, the parameter optimization in the proposed model follows an alternating manner. Such a strategy can significantly reduce the computation burden. Mathematically, given a weight function  $w$  with parameters  $\gamma_t$ , the update of  $\theta_{t+1}$  can be obtained by the following equation:

$$\theta_{t+1} = \theta_t - \eta_{\theta} \nabla_{\theta} A(\theta_t, \gamma_t) \quad (12)$$

where,  $\eta_{\theta}$  is the learning rate for classifier network. Then, following (11),  $\gamma_{t+1}$  can be formulated as:

$$\gamma_{t+1} = \gamma_t - \eta_{\gamma} \nabla_{\gamma} B(\theta_{t+1}) \quad (13)$$

Follow the chain rule, the gradient of  $B(\theta_{t+1})$  can be reformulated as  $\nabla_{\theta} B(\theta_t) - \eta_{\theta} \nabla_{\gamma} \nabla_{\theta} A(\theta_t, \gamma_t)$ . To efficiently calculate this, an automatic differentiation strategy is applied [33]. Basically, for each iteration, the local descent directions of the training data are first examined on the training loss surface. Then, they are recalculated based on their similarity to the descent directions of the supervised loss surface. This strategy requires two full forward and backward passes of the network on training loss and supervised loss for parameter update, respectively. The first forward and backward pass is used to calculate the loss using  $A(\theta_t, \gamma_t)$  and obtain  $\nabla_{\theta} A(\theta_t, \gamma_t)$ . Then, model parameter  $\theta_{t+1}$  can be updated using (12). The weight function is then subjected to the second forward and backward pass in order to calculate the loss using  $B(\theta_{t+1})$  and  $\nabla_{\gamma} B(\theta_{t+1})$ . After that,  $\gamma_{t+1}$  can be updated using (13). Finally, the last forward and backward pass

<sup>7</sup>For each  $\gamma$ , we need to compute the optimal  $\hat{\theta}$ . The computational complexity is  $O(n^2)$ . Thus, each single loop can be very expensive.

---

### Algorithm 1: Safe Event Classifier Training using Automatic Differentiation.

---

**Require:** Labeled data  $N_l = \{(x_1, y_1), \dots, (x_m, y_m)\}$ ; unlabeled data  $N_u = \{x_{m+1}, \dots, x_{m+k}\}$ ; initial model parameter  $\theta_0$ ; initial weight function parameter  $\gamma_0$ ; learning rate for model parameter  $\eta_{\theta}$ ; learning rate for weight function parameter  $\eta_{\gamma}$ ; iteration number  $T$ .

- 1: **for**  $t = 0, \dots, T - 1$  **do**
  - 2:     Select sample batch from  $N_l \rightarrow \{x_l, y_l\}$ .
  - 3:     Select sample batch from  $N_u \rightarrow \{x_u\}$ .
  - 4:     Compute generalization loss and weighted empirical loss using (7)  $\rightarrow A(\theta_t, \gamma_t)$ .
  - 5:     Calculate the gradient of model parameter  $\rightarrow \nabla_{\theta} A(\theta_t, \gamma_t)$ .
  - 6:     Update model parameter using  $\eta_{\theta}$  and (12)  $\rightarrow \theta_{t+1}$ .
  - 7:     Recompute generalization loss using (9).
  - 8:     Calculate the gradient of weight function parameter  $\rightarrow \nabla_{\gamma} B(\theta_{t+1})$ .
  - 9:     Update weight function parameter using  $\eta_{\gamma}$  and automatic differentiation strategy  $\rightarrow \gamma_{t+1}$ .
  - 10: **end for**
- 

is performed to minimize the reweighted objective to finish one iteration. Note that this process can be easily implemented using popular deep learning frameworks such as TensorFlow [34]. See Algorithm 1 and [33] for more details.

### C. Pseudo Label Dropout

During the training process, based on the estimated results of three safe event identifiers, a part of unlabeled events will be labeled and added into the training dataset. In this work, a dropout strategy is applied in pseudo labeling to exclude those pseudo-labels with low confidence and ensure the stability of the training set during the training process. Specifically, each classifier is used to estimate the label of  $x_i$  for  $W$  times throughout each iteration and record the frequency  $\omega$  at which the outcome differs from the rest of the classifiers. When  $\omega < \frac{W}{3}$ , this pseudo label is recognized as a stable label and can be utilized for model retraining. As the value of  $W$  gets larger, it takes longer to estimate the pseudo labels in each iteration, thus greatly increasing computational burden. In other words, the selection of  $W$  is a trade-off between the stability of the pseudo labels and computational burden. In this work, different values of  $W$  are tested based on the performance of the validation set. The appropriate value of  $W$  is obtained when the accuracy of the validation set no longer increases significantly. Here, the value of  $W$  is assigned as 12.

## V. NUMERICAL RESULT

This section investigates the performance of our framework utilizing PMU data and related event logs from Western Interconnection. The full dataset consists of 4,800 data points taken under normal behaviors as well as 4,800 recorded events,



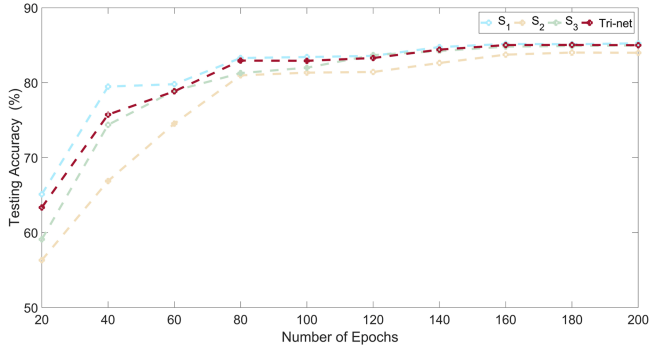


Fig. 5. Results of the proposed model's testing using 20% labeled events.

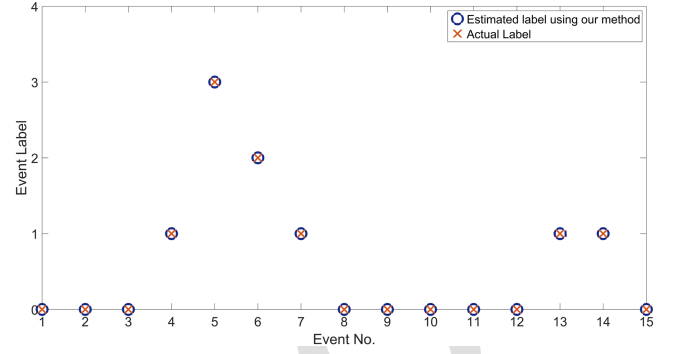


Fig. 6. Comparison of estimated event type and actual event type using the proposed method.

642 such as line outages, frequency events, and transformer outages.  
 643 To simulate a situation when the utility only captured a few  
 644 occurrences, the event labels are kept for 25% of the records  
 645 after data pre-processing. The remaining 75% of the event labels  
 646 were regarded as being unidentified. This process is completely  
 647 random. Considering that this dataset is an imbalanced dataset  
 648 (i.e., more than 75% of the events are line outages), we randomly  
 649 select 25% of the data samples for each type of event as labeled  
 650 data for the purpose of model training and testing, instead of  
 651 randomly selecting 25% of the data points in the entire dataset.  
 652 Note that a similar data partitioning strategy is also applied to  
 653 control the size of the labeled dataset in sensitivity experiments.  
 654 The available dataset is then evenly divided into  $k$  equal folds,  
 655 taking into account the PMU measurements and associated event  
 656 labels. In this work, the value of  $k$  is selected as 5. Based on these  
 657 partitioned folds, the proposed model is trained and tested in  $k$   
 658 iterations. In each iteration, one fold is left for testing and the  
 659 model is trained on the remaining  $k - 1$  folds. With this strategy,  
 660 it is possible to evaluate the performance of the suggested model  
 661 using all of the available data as unseen data.

#### 662 A. Effectiveness of the Proposed Method

663 The accuracy achieved from each iteration is averaged to  
 664 assess the model performance using the  $k$ -fold cross validation  
 665 strategy. The accuracy is calculated as follows:

$$666 \text{ Accuracy} = \frac{(TP + TN)}{(TP + FP + FN + TN)} \quad (14)$$

667 Where, FP stands for the false positive (e.g., event type is inferred  
 668 as frequency event while its true state is normal). TN is the true  
 669 negative (e.g., system state is inferred to be normal while its true  
 670 state is normal). FN for the false negative (i.e., system state is  
 671 inferred to be normal while its actual type is frequency event).  
 672 TP refers to the true positive (e.g., event type is inferred to be  
 673 a frequency event while its actual type is also frequency event).  
 674 In Fig. 5, testing results for the three safe event classifiers and  
 675 the suggested tri-network technique are shown. It can be seen  
 676 that the single safe classifier has an accuracy range of 84 to 85%  
 677 and the final testing accuracy of the tri-net method converges  
 678 to about 85%. This result indicates that the proposed triple  
 679 net framework is reliable and all classifiers converge to similar  
 accuracy regions. Additionally, Fig. 6 displays the actual and

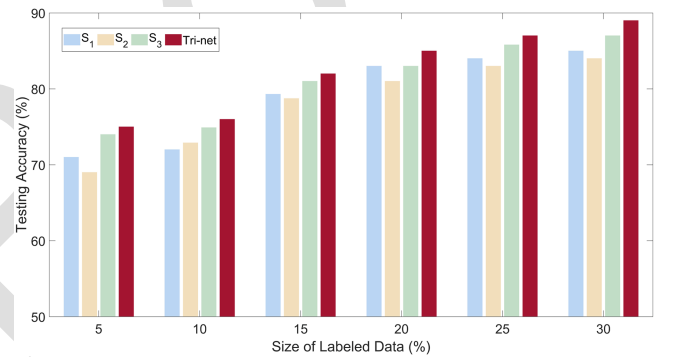


Fig. 7. Results of the sensitivity analysis using the proposed method.

680 estimated labels for 15 example events. As can be observed,  
 681 the proposed method successfully categorizes the various event  
 682 categories. It is noteworthy that these results are obtained with  
 683 only 25% of the labeled events.

#### 684 B. Sensitivity Analysis

685 To demonstrate how sensitive the proposed framework is to  
 686 the number of labeled events, the average accuracy with varied  
 687 quantities of labeled events is assessed and determined. As a  
 688 result of the loss of event information, the event classifier's  
 689 performance is expected to degrade as the volume of labeled data  
 690 diminishes. In this case study, we gradually increase the number  
 691 of labeled events from 5% to 30% (i.e., a total of 6 cases). The  
 692 results are presented in Fig. 7. For each case, testing accuracy  
 693 is calculated for  $S_1$ ,  $S_2$ ,  $S_3$  and tri-network, respectively. As  
 694 can be seen in the figure, as the percentage of labeled data rises  
 695 from 5% to 30%, the model's accuracy is gradually improved.  
 696 When the 30% of labeled events are available, the accuracy of  
 697 the proposed method is close to 90%. Meanwhile, it is clear  
 698 that the accuracy of the three modules is different, which proves  
 699 the effectiveness of our model diversity strategy. By combin-  
 700 ing these three modules, a better generalization capability can  
 701 be achieved. Compared to the previous study using the same  
 702 dataset [13], the proposed method requires only a much smaller  
 703 labeled dataset to achieve similar accuracy. Thus, the high-value  
 704 use case of our algorithm is when the utility has only a very small

TABLE I  
STATISTICAL ANALYSIS OF EVENT IDENTIFICATION

% of Labeled Data	Recall	Precision	$F_1$	MCC
5%	0.71	0.65	0.67	0.6
10%	0.76	0.66	0.69	0.64
15%	0.81	0.75	0.76	0.73
20%	0.83	0.79	0.81	0.77
25%	0.85	0.8	0.82	0.78
30%	0.86	0.83	0.84	0.81

number of labeled events (e.g., 5% of the total recorded events), the proposed method can still achieve 75% accuracy and provide meaningful help.

As an imbalanced classification task, it is crucial to show that the proposed method can correctly categorize each event type. Therefore, for each event type, several statistical metrics, including recall, precision,  $F_1$  score, and Matthews correlation coefficient (MCC) are utilized to further evaluate the performance of our method with different amounts of labeled data [35]. Specifically, recall is thought of as the percentage of relevant events that are correctly identified. Its dual metric, precision, is defined as the fraction of identified events that are relevant.  $F_1$  score can be considered as the harmonic average of the precision and recall:

$$F_1 = \frac{(\beta^2 + 1) * Prec * Recall}{(\beta^2 * Prec + Recall)} \quad (15)$$

where,  $\beta$  is the precision weight which is set at 1 in this paper.  $F_1$  score ranges in [0,1], where the maximum is reached when  $FN = FP = 0$ .  $F_1$  score is not defined based on confusion matrix since it is independent from  $TN$ . Meanwhile, it is not symmetric for type swapping. In comparison, MCC is a contingency matrix method of calculating the Pearson productmoment correlation coefficient in terms of the entries of confusion matrix:

$$MCC = \frac{TP*TN - FP*FN}{\sqrt{(TP+FP)(TP+FN)(TN+FP)(TN+FN)}} \quad (16)$$

MCC ranges in  $[-1, 1]$ , where 1 shows a perfect event identification, 0 corresponds to the random identification, and  $-1$  indicates total disagreement between estimated labels and actual labels. The average values of these indexes are presented in Table I. It is clear that the values of all metrics are at the same level. This result shows that the proposed method is able to handle the imbalance of the dataset and obtain stable estimation results for different kinds of events.

### C. Performance of the Proposed Method With Class Mismatch Problem

To demonstrate the performance of the proposed method with the class mismatch problem, we assume a special case where the utility never records a certain event type, but this event type appears in large numbers in unlabeled events. Specifically, all events belonging to the line outage are first excluded from the labeled dataset and then added to the unlabeled events proportionally. Only the remaining types of events (i.e., normal

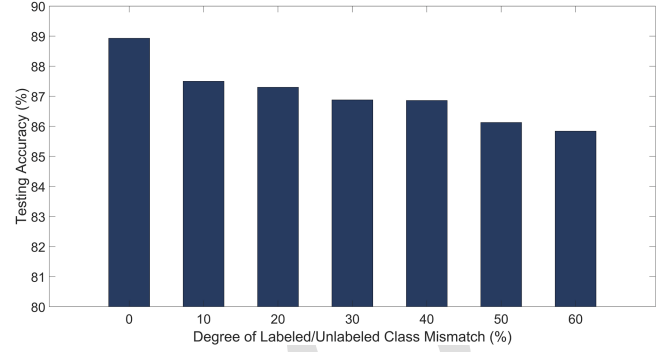


Fig. 8. Event identification accuracy of the proposed method with varying class mismatch degrees.

operation data, XFMR outages, and frequency events) are used for initial model training. As training proceeds, our model is expected to avoid pseudo-labeling hidden line outage events and adding them to the training set, thus preventing performance degradation. Here, we gradually increase the degree of labeled and unlabeled class mismatch degree from 0% to 60% to test the effectiveness of our algorithm, respectively. Note that the degree of labeled/unlabeled class mismatch is obtained by the ratio of the number of line outage events (i.e., unknown events) to the number of other kinds of events (i.e., known events) among the unlabeled events. This degree can be equivalently viewed as the exploration value of unlabeled events. In the extreme case, when this degree is 100%, it means that no unlabeled events should be exploited in model training. The results are presented in Fig. 8. As shown in the figure, it can be found that the accuracy of the algorithm slightly decreases as the degree of class mismatch increases. When unknown events accounted for half of the unlabeled events, the accuracy of our algorithm dropped by roughly 3% (from 89% to 86%). However, in this extreme case, our algorithm still performs better than the supervised learning-based event identification method (i.e., 82%) [13]. These findings corroborate the premise of this study, according to which the performance of the proposed framework diminishes with increasing class distribution mismatch between labeled and unlabeled data but never performs worse than that of the supervised learning method.

### D. Method Comparison

Considering that most existing works on event identification rely on unsupervised techniques (i.e., clustering algorithms) to connect unlabeled data and labeled data, We have conducted numerical comparisons with two clustering algorithms (i.e., hierarchical clustering and spectral clustering) previously used for event identification tasks [21], [36], [37]. Moreover, two state-of-the-art semi-supervised classification algorithms, PI model and mean teacher, are included in our comparison experiments to observe whether our models can perform better than previous semi-supervised learning models in the presence of high class mismatch degree [31], [38]. To ensure a fair comparison with unsupervised learning methods, the total number of event types in the set of unlabeled events is unknowable. In other

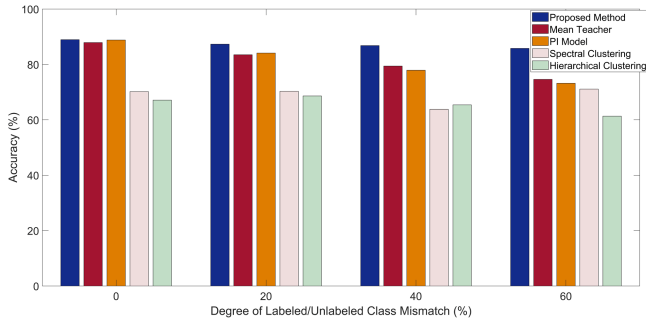


Fig. 9. Comparison results of five event identification methods.

words, the number of clusters is not available. Hence, in the experiments, the Davies-Bouldin validation index is applied to calibrate the unsupervised learning method to find the number of clusters [39]. The identification accuracy is calculated based on the misclassification between the true labels and the clustered labels. Like the last case, all methods are tested with varying class mismatch degrees. The comparison results are demonstrated in Fig. 9. It can be observed that the three semi-supervised learning methods generally outperform unsupervised learning methods, especially in the cases of low mismatch degree. The reason behind this is that the unsupervised learning methods do not use any labeling information, but only the data itself. This makes their results generally poor under the event classification task. Meanwhile, in some tests, we cannot obtain the correct number of clusters in a calibrated manner, which further reduces the accuracy. Among the semi-supervised learning methods, the proposed method performs better than the two state-of-the-art methods, especially when the mismatch degree is high. In some extreme cases (e.g., mismatch degree is 60%), the proposed algorithm still performs better than supervised learning-based methods, but other semi-supervised methods show performance degradation. Note that unsupervised learning models do not suffer from the class mismatch problem, as they do not care about label information.

### E. Computational Complexity Analysis

To demonstrate the practical complexity of the proposed algorithm, we conducted the case study on a typical personal computer. Based on our multiple experiments, when the event labels are retained for 25% of the records, the training computation of the proposed model time ranges from 1.7 hours to 1.9 hours. It should be noted that the training time also changes slightly with the volume of labeled data due to the pseudo-labeling process. The proposed method's average test time, based on 1,440 test samples, is roughly 0.8 ms. As a result, in a real grid, our method may deliver estimates in around 0.1 seconds after the PMU measurements arrive at the phase data concentrator after accounting for the communication delay. This is still much faster than the vast majority of heuristic-based methods.

## VI. CONCLUSION

In this paper, we design a novel data-driven method to accurately identify events using a limited number of labeled events and a rich set of unlabeled events. Our approach is built on a semi-supervised learning framework with three event identifiers. By designing a weight function, each classifier can selectively explore unlabeled events to provide additional information about the shape of the decision boundary among different event types. The proposed method can address two main challenges in power system event identification: 1) poor generalization of deep learning models caused by the limited number of labeled events. 2) class distribution mismatch problem between labeled events and unlabeled events caused by event data scarcity. The proposed solution has been successfully tested on an actual Western Interconnection dataset.

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