Enriching Load Data Using Micro-PMUs and Smart Meters

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Abstract-In modern distribution systems, load uncertainty 1 2 can be fully captured by micro-PMUs, which can record high-3 resolution data; however, in practice, micro-PMUs are installed 4 at limited locations in distribution networks due to budgetary 5 constraints. In contrast, smart meters are widely deployed but 6 can only measure relatively low-resolution energy consumption, 7 which cannot sufficiently reflect the actual instantaneous load ⁸ volatility within each sampling interval. In this paper, we have 9 proposed a novel approach for enriching load data for service 10 transformers that only have low-resolution smart meters. The key 11 to our approach is to statistically recover the high-resolution load ¹² data, which is masked by the low-resolution data, using trained 13 probabilistic models of service transformers that have both high-14 and low-resolution data sources, i.e., micro-PMUs and smart 15 meters. The overall framework consists of two steps: first, for the 16 transformers with micro-PMUs, a Gaussian Process is leveraged 17 to capture the relationship between the maximum/minimum load 18 and average load within each low-resolution sampling interval of 19 smart meters; a Markov chain model is employed to charac-20 terize the transition probability of known high-resolution load. 21 Next, the trained models are used as teachers for the transform-22 ers with only smart meters to decompose known low-resolution 23 load data into targeted high-resolution load data. The enriched 24 data can recover instantaneous load uncertainty and significantly 25 enhance distribution system observability and situational aware-26 ness. We have verified the proposed approach using real high-27 and low-resolution load data.

Index Terms—Distribution system, load uncertainty, micro PMU, smart meter, data enrichment.

I. INTRODUCTION

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³¹ A S THE advanced metering infrastructure (AMI) has been ³² widely deployed in distribution systems in recent years, ³³ utilities have gained access to large amounts of smart meter ³⁴ (SM) data [1]. To take advantage of this data, which is ³⁵ both spatially and temporally fine-grained, researchers and ³⁶ industry practitioners have performed time-series power flow

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Fig. 1. A one-day real service transformer load curve with 1-second load data and the corresponding hourly average load curve.

studies for optimizing network operation, expansion [2], [3], 37 and integrating renewable energy resources [4]. In many 38 cases, customer-level demands are aggregated to obtain 39 service transformer-level loads for performing power flow 40 studies [2], [5]. However, the problem is that in most cases, 41 SMs have a low sampling rate, e.g., one to four samples per 42 hour. Thus, the average demand measured at such low res-43 olutions cannot faithfully represent the uncertainties of the 44 instantaneous load. As illustrated in Fig. 1 for an exemplary 45 transformer, the maximum 1-second load data has reached 46 values 40% times larger than the corresponding hourly SM 47 reading within the same sampling interval. Also, compared to 48 the hourly measurements, the instantaneous load shows a high 49 level of variability, which has not been captured by the SMs. 50 Therefore, recovering the *masked* high-resolution load data is 51 critical in enhancing distribution system situational awareness 52 and granularity of modeling. 53

To further demonstrate the usefulness of high-resolution 54 load data, we primarily focus on three specific applications. 55 First, accurate power flow analysis requires high-resolution 56 load data. Power flow analysis is critically important for util-57 ities. It can provide voltage profiles, which can help utilities plan new circuits, add customers, and track and fix voltage 59 problems. Since load is an essential component in distribu-60 tion systems, high-resolution load profiles play a critical role 61 in obtaining power flow solutions with high fidelity. In con-62 trast, the 15-min, 30-min, or 1-hour load data might cause 63 unacceptable errors [6], [7]. This is why most utilities take 64 conservative approaches in distribution system operation and 65 planning. Instead, taking full advantage of high-resolution load 66 data can free utilities from conservative measures. Second, 67 accurate voltage regulation analysis requires high-resolution 68

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69 load data. In many cases, utilities perform time-series power 70 flow analysis to examine the actions of voltage regulation 71 devices. Typical voltage regulation devices include voltage 72 regulators and capacitors. The controller of these two types of 73 devices usually has a time delay before executing a regulating 74 order. By doing this, the voltage regulation devices can avoid ⁷⁵ unnecessary frequent reactions to fast and temporary voltage ⁷⁶ transients. The time delay is typically around 30 seconds. 77 Therefore, to accurately capture the response of voltage regu-78 lation devices, the time resolution of load data for performing 79 time-series power follow analysis should match the delay time 80 of regulation devices' controller [6], [8]. Third, high-resolution ⁸¹ load data can facilitate photovoltaic (PV) integration. In most 82 cases, utilities conservatively maintain customer voltages very 83 close to the upper bound of the ANSI voltage range due to 84 conservative considerations. Under this condition, even though ⁸⁵ the load increase may cause a voltage drop, the voltage will ⁸⁶ still be within the ANSI voltage range and satisfy voltage qual-⁸⁷ ity requirements. However, under such conservative operation 88 logics, new PV integration can cause over-voltages. To assess 89 the impact of PV generation, one promising way is to uti-90 lize high-resolution (1-second or 1-min) PV generation data 91 to perform power flow analysis, because low-resolution data ⁹² might fail to capture PV output variations. Since the load varia-⁹³ tions might not be negligible in some scenarios, it is necessary 94 to combine high-resolution load data and PV output data to 95 perform time-series power flow analysis [9], [10].

There is only a limited number of previous works focus-96 97 ing on load data enrichment. In [8], a top-down method is ⁹⁸ presented to generate service transformer-level high-resolution 99 load profiles. First, low-resolution substation load profiles 100 are allocated to service transformers via scaling. Then, the 101 allocated profiles are decomposed into high-resolution load 102 data by aggregating typical load patterns stored in variabil-¹⁰³ ity and diversity libraries. In [11], synthetic load datasets are 104 created for four typical seasonal months using captured vari-105 ability from high-resolution service transformer load data. To 106 develop rich load data, researchers have added random noise to load data for modeling load uncertainty, as presented in [12]. 107 ¹⁰⁸ In [13], a discrete wavelet transform (DWT)-based approach 109 is proposed to parameterize intra-second variability of high-110 resolution transformer load data. To sum up, the primary 111 limitations of previous load data enrichment methods are: the 112 scaled substation load profiles allocated to service transformers 113 differ from the actual load profiles since each transformer has a 114 distinct load pattern [14], inaccuracy of adding random noise, 115 and lack of specific methodology for applying the extracted 116 load variability [7].

Considering the shortcomings of previous works, in this paper, we have developed a novel *bottom-up* approach for enriching hourly load data for service transformers that only have SMs, by leveraging the high-resolution load data of service transformers with micro-PMUs and SMs. This concept is illustrated in Fig. 2, where the service transformer in the middle with rich load data is utilized to perform load data enrichment for the other two service transformers with only SMs. Before proceeding to specific steps, we have observed that each low-resolution load observation corresponds to a *segment*



Fig. 2. Schematic diagram of a radial distribution feeder with diverse sensors.



Fig. 3. Overall structure of the proposed load data enrichment approach.

of high-resolution load profile, as shown in Fig. 1. Therefore, 127 enriching one known low-resolution load observation comes 128 down to determining the maximum and minimum loads in the 129 corresponding high-resolution load profile segment and infer- 130 ring how the instantaneous load varies within those bounds. To 131 do this, the proposed approach exploits learned probabilistic 132 models that are trained using the high-resolution load data of 133 service transformers with micro-PMUs. Thus, the first stage is 134 to train probabilistic models using known high-resolution load 135 data of micro-PMUs. Specifically, a Gaussian Process is used 136 to capture the relationship between the maximum/minimum 137 bound and the average load. A Markov process is leveraged to 138 model the probabilistic transition of instantaneous load within 139 the bounds. These trained models for transformers with micro- 140 PMUs form a *teacher* repository. The second stage is to extend 141 the trained probabilistic models to the service transformers that 142 only have SMs, i.e., the students, for enriching low-resolution 143 load data. Specifically, the trained Gaussian Process models 144 are employed to estimate the unknown maximum/minimum 145 bound using the known low-resolution observation as the 146 input, and the trained Markov models are used to probabilis-147 tically determine the variability of instantaneous load within 148 the estimated maximum and minimum bounds. In addition, the 149 load enrichment process in the second stage is performed using 150 a weighted averaging operation, where the weights are determined by evaluating the similarity between low-resolution load 152 data of the student and teacher transformers. Our approach 153 is not restricted to the condition that the teacher and stu-154 dent transformers should have the same rating, loss, or served 155 customer number. The overall framework of our proposed 156 approach is illustrated in Fig. 3. 157

The primary contribution of our paper is that we have 158 proposed a novel bottom-up inter-service-transformer load 159 data enrichment approach using micro-PMUs and SMs. Our 160 method takes full advantage of the fine-grained spatial and 161 temporal granularity of SM and micro-PMU data. The rest 162 of the paper is organized as follows: Section II presents the 163 process of training teacher models using data from transformers with micro-PMUs. Section III describes the procedure of 165 enriching load data for transformers with only SMs using 166



Fig. 4. Observation from real high-resolution load data for a service transformer.

¹⁶⁷ the trained teacher models. In Section IV, case studies are ¹⁶⁸ analyzed, and Section V concludes the paper.

II. CONSTRUCTING A REPOSITORY OF TEACHER TRANSFORMERS

The first step in load data enrichment is to train inferreal models based on high-resolution micro-PMU load data. In this section, inference model training includes two stages: load boundary inference model training, and load variability parameterization. Also, keep in mind that the inference model training process is performed for *each* service transformer with a micro-PMU.

178 A. Training Load Boundary Inference Model

Based on real high-resolution load data, we have observed 179 180 that the average load over each low-resolution sampling ¹⁸¹ interval, P_a , and the corresponding maximum/minimum load within that interval demonstrate a nonlinear relationship, as 182 183 shown in Fig. 4. Note that *P* and *P* denote the upper and lower 184 bounds of instantaneous load within each sampling interval, 185 respectively. Considering this, the Gaussian Process regression 186 (GPR) technique, which shows excellent flexibility in captur-¹⁸⁷ ing nonlinearity, is leveraged to train load boundary inference 188 models [15]. One primary reason for choosing GPR is that 189 after running numerical tests, it demonstrated a relatively 190 better performance when applied to our dataset than some 191 other state-of-the-art nonlinear regression models, such as the 192 Support Vector Machine model and the Polynomial regres-¹⁹³ sion model. Note that other regression models with acceptable ¹⁹⁴ accuracy can also be integrated into our proposed framework 195 for load data enrichment. The basic idea behind GPR is that ¹⁹⁶ if the distance between two explanatory variables is small, we 197 have high confidence that the difference between correspond-¹⁹⁸ ing dependent variables will be small as well. Specifically, ¹⁹⁹ using GPR, the upper bound of instantaneous load within the 200 t'th hour, P(t), as a function of the hourly average load can 201 be written as:

$$P(t) = f(P_a(t)), \tag{1}$$

²⁰³ where, $P_a(t)$ denotes the average load over the t'th hour. ²⁰⁴ Unlike deterministic approaches, where $f(P_a(t))$ is assumed to ²⁰⁵ yield a single value for each $P_a(t)$, in GPR, $f(P_a(t))$ is a ran-²⁰⁶ dom variable. Intuitively, the distribution of $f(P_a(t))$ reflects the uncertainty of functions evaluated at $P_a(t)$. In GPR, the 207 function $f(P_a(t))$ is distributed as a Gaussian process: 208

$$f(P_a(t)) \sim \mathcal{GP}(\mu(P_a(t)), K(P_a(t), P_a(t'))), \qquad (2)$$

where, $\mu(P_a(t))$ reflects the expected value of the maxi- ²¹⁰ mum load inference function, and the covariance function ²¹¹ $K(P_a(t), P_a(t'))$ represents the dependence between the max- ²¹² imum loads during different hour intervals. In our problem, ²¹³ the covariance function $K(\cdot, \cdot)$ is specified by the Squared ²¹⁴ Exponential Kernel function expressed as: ²¹⁵

$$K(P_a(t), P_a(t')) = \sigma_f^2 \exp\left(-\frac{||P_a(t) - P_a(t')||_2^2}{2\lambda^2}\right), \quad (3) \text{ 216}$$

where, $||\cdot||_2$ represents l_2 -norm, σ_f and λ are hyper-parameters, ²¹⁷ which are determined using cross-validation. Intuitively, (3) ²¹⁸ measures the distance between $P_a(t)$ and $P_a(t')$, which can ²¹⁹ also reflect the similarity between $\overline{P}(t)$ and $\overline{P}(t')$, as shown ²²⁰ in Fig. 4. For each service transformer with a micro-PMU, ²²¹ the average load and corresponding maximum load during each hour interval are known and provide a training ²²³ dataset. Thus, applying (2) to the entire training dataset ²²⁴ ($P_a(1), \overline{P}(1)$), ..., ($P_a(N), \overline{P}(N)$), an *N*-dimensional joint ²²⁶ Gaussian distribution can be constructed as: ²²⁷

$$\begin{bmatrix} f(P_a(1)) \\ \vdots \\ f(P_a(N)) \end{bmatrix} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma}), \qquad (4) \ _{226}$$

where

$$\boldsymbol{\mu} = \begin{bmatrix} \mu(P_a(1)) \\ \vdots \\ \mu(P_a(N)) \end{bmatrix}, \qquad (5a) \ _{236}$$
$$\boldsymbol{\Sigma} = \begin{bmatrix} K(P_a(1), P_a(1)) & \cdots & K(P_a(1), P_a(N)) \\ \vdots & \ddots & \vdots \end{bmatrix}. (5b) \ _{237}$$

$$\begin{bmatrix} \vdots & \vdots & \vdots \\ K(P_a(N), P_a(1)) & \cdots & K(P_a(N), P_a(N)) \end{bmatrix}$$

The joint Gaussian distribution formulated in (4) represents a ²³² trained nonparametric *maximum* load inference model. Also, ²³³ the same procedure can be applied to the hourly average ²³⁴ and minimum load pairs, { $(P_a(1), \underline{P}(1)), \ldots, (P_a(N), \underline{P}(N))$ }, ²³⁵ to obtain a trained nonparametric *minimum* load inference ²³⁶ model. ²³⁷

In summary, for each service transformer with a micro-PMU, we can obtain two trained GPR models for inferring the maximum and minimum loads based on the corresponding hourly average load measured at the low-resolution sampling intervals. 242

B. Training Load Variability Inference Model

Given an hourly average load observation, simply determining load boundaries is not sufficient for load data enrichment. ²⁴⁵ We also have to learn how the load varies within these bounds. ²⁴⁶ It is observed from real high-resolution load data that when an ²⁴⁷ appliance is turned on, the load will jump to a certain level, as ²⁴⁸ shown in Fig. 5. This process can be modeled as the Markov ²⁴⁹ chain, which represents a system transitioning from one state ²⁵⁰

229

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Fig. 5. Load variations within a day captured by high-resolution data.

²⁵¹ to another over time. Also, it is observed from Fig. 5 that once ²⁵² the load has transitioned to a certain level, it will stay almost ²⁵³ invariant for a certain period of time. Therefore, the load state ²⁵⁴ duration demonstrates statistical properties, and there exists a ²⁵⁵ temporal correlation in state transition. Considering this, we ²⁵⁶ have employed a second-order Markov model to capture the ²⁵⁷ stochastic variability of the instantaneous load. Markov chains ²⁵⁸ of second order are processes in which the next state depends ²⁵⁹ on two preceding ones.

Since load is continuous, the first step to parameterize a Markov chain process is to discretize *high-resolution* load measurements. Specifically, for the *i*'th high-resolution load observation during the *t*'th hour interval, the corresponding observed state is determined as:

265
$$S_t(i) = n_s, \quad n_s \in \{1, \dots, N_s\}, t = 1, \dots, N,$$

266 if $(n_s - 1) \frac{\overline{P}(t) - \underline{P}(t)}{N_s} \le P_t(i) - \underline{P}(t) < n_s \frac{\overline{P}(t) - \underline{P}(t)}{N_s},$
267 (6)

²⁶⁸ where, N_s represents the total number of the unique discrete ²⁶⁹ states and $P_t(i)$ is the *i*'th instantaneous load measurement ²⁷⁰ during the *t*'th hour.

Also, it is observed from real high-resolution load data 271 272 that different load levels display different stochastic processes. 273 Typically, an air-conditioner cyclically starts and stops in 274 the order of minutes. In contrast, the baseload, which is 275 often caused by lighting and electronic devices, shows signif-276 icantly longer cycles. In addition, the air-conditioning devices 277 and baseload appliances show different average load levels 278 over low-resolution sampling intervals due to different capaci-279 ties. Therefore, to capture the different transition processes, 280 the discretized observation states need to be divided into multiple subsets according to the hourly average load mea-281 282 surements. Each subset is used to train a Markov chain 283 model. Specifically, first, the entire collection of discretized observation states is split into N_d subsets according to the 284 ²⁸⁵ corresponding low-resolution load observation, $P_a(t)$. The j'th 286 subset is obtained as:

²⁸⁷
$$\boldsymbol{D}_{j} = \{S_{t}(i)\}, \quad i \in \{1, \dots, N'\}, t \in \{1, \dots, N\},$$



Fig. 6. Representation of the 3D probability transition matrix.

if
$$F\left(\frac{(j-1)\times 100}{N_d}\right) \le P_a(t) < F\left(\frac{j\times 100}{N_d}\right)$$
, (7) 280

where, $F(\cdot)$ is a function that returns percentiles of the entire ²⁸⁹ set of low-resolution load observations, and N' is the total ²⁹⁰ number of discretized observation states in each low-resolution ²⁹¹ sampling interval. ²⁹²

Then, for each subset D_j , the stochastic process is parameterized by empirically estimating the transition probabilities 294 between discrete observed states in terms of a transition 295 matrix. A second-order Markov process consists of three 296 states: the previous state, the current state, and the next state. 297 Therefore, the stochastic transition matrix, P_r , is a threedimensional (3D) array, as illustrated in Fig. 6. Each element 299 of P_r , $P_r(x, y, z)$, represents the probability of moving to state 300 z under the condition that the previous state is x and the current 301 state is y. For each subset D_j , elements of P_r can be estimated 302 from the frequencies of posterior states. Assume D_j takes on 303 the form of $\{S(i)\}, i = 1, ..., N'_s$, where N'_s is the total number of observation states in D_j , then the occurrence number at 305 (x, y, z) can be counted as: 306

$$\boldsymbol{n}(x, y, z) = \sum_{i=2}^{N_s - 1} \left[S(i - 1) = x \text{ and} \right]$$

$$S(i) == y \text{ and } S(i+1) == z],$$
 (8) 308

322

where, $[\cdot]$ is the Iverson bracket which converts any logical ³⁰⁹ operation into 1, if the operation is satisfied, and 0 otherwise. ³¹⁰ "==" stands for the "equal to" operator and "*and*" is the log-³¹¹ ical and operator. Thus, the elements of transition probability ³¹² matrix are computed by: ³¹³

$$\boldsymbol{P}_{r}(x, y, z) = \frac{\boldsymbol{n}(x, y, z)}{\sum_{z} \boldsymbol{n}(x, y, z)}, \quad x, y = 1, \dots, N_{s}.$$
 (9) 314

For *each* subset D_{j} , $j = 1, ..., N_d$, (9) is performed to obtain ³¹⁵ a 3D stochastic transition matrix. Moreover, for *each* service ³¹⁶ transformer with a micro-PMU, the entire above-mentioned ³¹⁷ procedure for parameterizing variability is conducted to obtain ³¹⁸ N_d stochastic transition matrices. ³¹⁹

III. ENRICHING LOAD DATA FOR TRANSFORMERS WITH 320 ONLY SMART METERS 321

A. Determining Teacher Weights

Recall that our goal is to recover the high-resolution load ³²³ data masked by the low-resolution load data. In this procedure, ³²⁴ we leverage teacher models of transformers with micro-PMUs ³²⁵ for service transformer with only SMs. Note that there might ³²⁶ 327 be more than one teacher transformer serving the same num-₃₂₈ ber of customers as the student transformer supplies. Different 329 teacher transformers have different load behaviors. Thus, it ³³⁰ is necessary to determine the learning weights corresponding particular teacher transformers. These weights are deterto 331 332 mined by evaluating customer-level load similarity between the teacher and student transformers using low-resolution load 333 data. 334

Specifically, for the *i*'th customer served by a student trans-335 ³³⁶ former, we can obtain a typical daily load pattern, P_i , which 337 reflects customer behavior and the total capacity of appli-338 ances [16]. Then, for a student transformer serving N_c cus-³³⁹ tomers, we can obtain N_c daily load patterns, $\{P_1, \ldots, P_{N_c}\}$. ³⁴⁰ Similarly, for a teacher transformer supplying N_c^k customers, ³⁴¹ we can obtain N_c^k daily load patterns. Since we have multiple 342 teacher transformers, we can obtain a set of load pattern 343 collections. The load pattern collection for the k'th teacher transformer is denoted by $\{\boldsymbol{P}_1^k, \ldots, \boldsymbol{P}_{N_c^k}^k\}, k = 1, \ldots, N_t$ ³⁴⁵ where, N_t is the total number of teacher transformers. Then, $_{346}$ load similarity between a student transformer and the k'th 347 teacher transformer is evaluated as:

³⁴⁸
$$W'_{k} = \frac{1}{N_{c}N_{c}^{k}}\sum_{i=1}^{N_{c}}\sum_{j=1}^{N_{c}^{k}}||\boldsymbol{P}_{i}-\boldsymbol{P}_{j}^{k}||, \quad k = 1, \dots, N_{t}, \quad (10)$$

 $_{349}$ where, N_c^k denotes the number of customers served by the k'th 350 teacher transformer. Thus, the teacher and student transform-351 ers do not necessarily serve the same number of customers. ₃₅₂ The W'_k 's in (10) are then normalized for a more convenient 353 mathematical representation:

 $W_k = \frac{W'_k}{\sum_{k=1}^{N_t} W'_k}.$

In summary, the normalized similarity weights reflect the 355 356 confidence of a student transformer to learn from multiple teacher transformers for load data enrichment. 357

358 B. Enriching Load Data

Using the normalized teacher weights, along with the 359 360 load boundary and variability inference models derived in Section II, we can conduct poor load data enrichment for 361 service transformers that only have SMs. 362

1) Inferring Load Boundaries: In Section II-A, for each 363 364 teacher transformer with high-resolution load data, we have 365 obtained two GPR models for inferring the maximum and min-³⁶⁶ imum loads given the corresponding average load over each 367 low-resolution sampling interval. These two models are non-³⁶⁸ parametric and expressed in (4). Specifically, the trained max-³⁶⁹ imum load inference model for the *k*'th teacher transformer is 370 expressed as:

371

354

$$\begin{bmatrix} \overline{P}_{k}(1) \\ \vdots \\ \overline{P}_{k}(N) \end{bmatrix} = \begin{bmatrix} f_{k}(P_{a,k}(1)) \\ \vdots \\ f_{k}(P_{a,k}(N)) \end{bmatrix} \sim \mathcal{N}(\boldsymbol{\mu}_{k}, \boldsymbol{\Sigma}_{k}).$$
(12)

372 To conduct load data enrichment, first, customer-level SM 373 data are aggregated to obtain the load supplied by the stu-³⁷⁴ dent transformer, namely, $\{P_{a,*}(1), \ldots, P_{a,*}(N)\}$. Note that





Fig. 7. Detailed steps of enriching load data.

Micro-PMU: $P_t^1(i), t = 1, ..., N$

Training

 $GPR_1^*'s$

 $\overline{P}_{1}(t), P_{a}^{1}(t)\},$

SM Data

Similarity Evaluation

 W_1 .

 P_j^1

 P_1

SM Data $P_{a*}^{1}(t)$,...

 $\Sigma P_{a,*}^i(t)$

Weighted Boundary Inference

 $P_{a,*}^{N_c}(t)$

 $P_{a,*}(t)$

 P_{N_c}

 $[\underline{P_*}(t), \overline{P_*}(t)]$

Similarity Evaluation

GPR

 $\{\underline{P_1}(t), P_a^1(t)\}$

Discretize

 $S_t^1(i)$

 $MKC_1^{*'s}$

MKC

(11)

the transformer loss is approximated and added to the aggre- 375 gate load. Specifically, the total loss of a student transformer 376 supplying an aggregate load, $P_{a,*}(t)$, is estimated as follows: 377

$$P_{l,*}(t) = P_{nll,*} + \frac{P_{a,*}^2(t)}{P_{rate,*}^2} P_{fll,*}, \quad t = 1, \dots, N, \quad (13) \text{ 378}$$

where, $P_{nll,*}$ and $P_{fll,*}$ denote the no-load loss and full-load 379 loss, respectively. Prate,* denotes the kVA rating of the stu- 380 dent transformer. $P_{nll,*}$, $P_{fll,*}$, and $P_{rate,*}$ are typically provided ³⁸¹ by transformer manufacturers. Note that the effect of reactive 382 power is ignored when estimating the loss because the reac- 383 tive power is typically small [7]. For conciseness, we assume 384 that $P_{a,*}(t)$ in the following sections has already included the 385 aggregate load and the corresponding total loss of the student 386 transformer. 387

Then, we assume the unknown upper bound of instan- 388 taneous load in terms of a function variable, $\overline{P}_{k,*}(t) = 389$ $f_k(P_{a,*}(t)), t = 1, \dots, N$, follows a Gaussian distribution. By 390 appending $\overline{P}_{k,*}(t)$ at the end of (12), an (N+1)-dimensional 391 Gaussian distribution can be formed as:

$$\begin{bmatrix} \overline{P}_{k}(1) \\ \vdots \\ \overline{P}_{k}(N) \\ \overline{P}_{k,*}(t) \end{bmatrix} = \begin{bmatrix} f_{k}(P_{a,k}(1)) \\ \vdots \\ f_{k}(P_{a,k}(N)) \\ f_{k}(P_{a,*}(t)) \end{bmatrix}$$

$$\sim \mathcal{N}\left(\begin{bmatrix} \boldsymbol{\mu}_{k} \\ \boldsymbol{\mu}_{*} \end{bmatrix}, \begin{bmatrix} \boldsymbol{\Sigma}_{k} & \boldsymbol{\Sigma}_{k*} \\ \boldsymbol{\Sigma}_{k*}^{T} & \boldsymbol{\Sigma}_{**} \end{bmatrix}\right), \quad (14) \quad {}_{394}$$

where, Σ_{k*} represents the training-test set covariances 395 and Σ_{**} is the test set covariance. In (14), observations 396 for $\{\overline{P}_k(1), \ldots, \overline{P}_k(N)\}$ are known and denoted by $\overline{p}_k = 397$

³⁹⁸ { $\overline{p}_k(1)$),..., $\overline{p}_k(N)$ }. Thus, using the Bayes rule, the distri-³⁹⁹ bution of $\overline{P}_{k,*}(t)$ conditioned on \overline{p}_k is obtained as:

400
$$\overline{P}_{k,*}(t)|\overline{p}_k \sim \mathcal{N}(\mu_*(t), \Sigma_*(t)), \tag{15}$$

⁴⁰¹ where, $\mu_*(t) = \boldsymbol{\Sigma}_{k*}^T \boldsymbol{\Sigma}_k^{-1} \bar{\boldsymbol{p}}_k$ and $\boldsymbol{\Sigma}_*(t) = \boldsymbol{\Sigma}_{**} - \boldsymbol{\Sigma}_{k*}^T \boldsymbol{\Sigma}_k^{-1} \boldsymbol{\Sigma}_{k*}$. ⁴⁰² Note that $\mu_*(t)$ denotes the most probable value of the esti-⁴⁰³ mated upper bound of instantaneous load given the average ⁴⁰⁴ load during each low-resolution sampling interval.

Since we have N_t teacher transformers, we can obtain 406 a total of N_t estimated maximum load candidates, namely, 407 { $\mu_*^1(t), \ldots, \mu_*^{N_t}(t)$ }. Also, considering load similarity between 408 the student transformer and teacher transformers, a weighted-409 averaging operation is performed on all the inferred maximum 410 loads to calculate a final estimated upper bound of instanta-411 neous load:

412
$$\overline{P}_{*}(t) = \sum_{k=1}^{N_{t}} W_{k} \mu_{*}^{k}(t), \quad t = 1, \dots, N.$$
 (16)

⁴¹³ The same procedure introduced above is also applied to ⁴¹⁴ infer the unknown minimum load, $\underline{P}_{*}(t)$, using the known aver-⁴¹⁵ age load over each low-resolution sampling interval. Once we ⁴¹⁶ have obtained the estimated load boundaries, then the trained ⁴¹⁷ probability matrices can be leveraged to infer load variability ⁴¹⁸ within each boundary.

419 2) Inferring Load Variability: As introduced in 420 Section II-B, each teacher transformer has N_d extracted 421 transition matrices corresponding to different load levels. 422 Therefore, the first step in inferring the unknown high-423 resolution load variability is to determine which transition 424 matrix to use. In other words, we need to find the variability 425 inference matrix corresponding to the load level that the 426 low-resolution load measurement belongs to. This is achieved 427 by splitting the known low-resolution load observations of 428 student transformer into N_d subsets:

429
$$P'_{*} = \{P_{a,*}(t)\}, \quad t \in \{1, \dots, N\}, j = 1, \dots, N_{d},$$

430 if $F\left(\frac{(j-1) \times 100}{N_{d}}\right) \le P_{a,*}(t) < F\left(\frac{j \times 100}{N_{d}}\right).$
431 (17)

⁴³² Then, the *j*'th stochastic transition matrix of each teacher ⁴³³ transformer is selected for enriching the low-resolution load ⁴³⁴ measurements in the *j*'th subset of the student transformer, ⁴³⁵ P_*^j . Moreover, considering that there is more than one teacher ⁴³⁶ transformer, i.e., for each subset P_*^j , we have N_t transition ⁴³⁷ matrices to use. Thus, before proceeding to instantaneous ⁴³⁸ load variability inference, a weighted averaging process sim-⁴³⁹ ilar to the load boundary estimation is conducted to obtain a ⁴⁴⁰ comprehensive transition modal:

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$$\boldsymbol{P}_{r*}^{j} = \sum_{k=1}^{N_{t}} W_{k} \boldsymbol{P}_{r}^{j,k}, \quad j = 1, \dots, N_{d}, \quad (18)$$

⁴⁴² where, $\boldsymbol{P}_{r}^{j,k}$ stands for the transition matrix for the *k*'th teacher ⁴⁴³ transformer based on the *j*'th subset of observation states, ⁴⁴⁴ \boldsymbol{D}_{j}^{k} . Then, for each low-resolution load measurement to be ⁴⁴⁵ enriched, $P_{a,*}^{j}(t)$, the final targeted transition matrix, \boldsymbol{P}_{r*}^{j} , and ⁴⁴⁶ the inferred load boundary, $\{\overline{P}_{*}^{j}(t), \underline{P}_{*}^{j}(t)\}$, are leveraged to generate the targeted high-resolution load data. Specifically, ⁴⁴⁷ assume the previous state is $S_{t,*}^{j}(i-1)$, and the current state ⁴⁴⁸ is $S_{t,*}^{j}(i)$, our goal is to determine the next state, $S_{t,*}^{j}(i+1)$, ⁴⁴⁹ where, $i = 1, \ldots, N'$, stands for the sequence number of states ⁴⁵⁰ within the *t*'th low-resolution sampling interval. To do this, ⁴⁵¹ first, a random value at *i*, $U_{*}(i)$, is generated from the uni-⁴⁵² form distribution within the interval (0, 1). Then, the state at ⁴⁵³ (*i* + 1) is determined by: ⁴⁵⁴

$$S'_{t,*}(i+1) = z_*, \quad i = 2, \dots, N' - 1,$$

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$$\text{if } \sum_{z=1}^{\infty} \boldsymbol{P}_{r*}^{j} \left(S_{t,*}^{j}(i-1), S_{t,*}^{j}(i), z \right) \le U_{*}(i) \qquad \text{456}$$

$$<\sum_{z=1}^{z_{*}}\boldsymbol{P}_{r*}^{j}\left(S_{t,*}^{j}(i-1),S_{t,*}^{j}(i),z\right).$$
(19) 457

Note that the generated $S_{t,*}^{j}(i)$'s are discrete state samples, 458 therefore, they need to be transformed to specific load samples: 459

$$P_{t,*}^{j}(i) = \underline{P}_{*}^{j}(t) + \frac{S_{t,*}^{j}(i) \left(\overline{P}_{*}^{j}(t) - \underline{P}_{*}^{j}(t)\right)}{N_{s}}, \qquad (20)$$

Since there is more than one low-resolution time interval, ⁴⁶² the above procedure is conducted for *each* low-resolution ⁴⁶³ load observation. Also, since the low-resolution load observations are grouped into multiple subsets, the entire procedure ⁴⁶⁵ introduced above is conducted through *all subsets* of lowresolution load measurements. The detailed steps for load data ⁴⁶⁷ enrichment for a student service transformer is illustrated in ⁴⁶⁸ Fig. 7. ⁴⁶⁹

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In this section, we have validated the proposed load data 471 enrichment approach using real high- and low-resolution load 472 data [17]. 473

A. Dataset Description

The dataset includes real 1-second load data for eight 475 service transformers and hourly SM energy data for 185 476 customers. Among these customers, 36 are supplied by the 477 8 transformers with high-resolution load data (with micro-PMUs), and the remaining 149 customers are fed by the other 479 34 service transformers with low-resolution load data (with 480 only SMs). To verify the performance of load data enrichment, the utility has also installed extra measuring devices to 482 record 1-second load data for the service transformers with 483 only SMs [17]. The time range of the dataset is two months. 484 In practice, micro-PMUs might have higher sampling rates 485 than one sample per second, however, there is no fundamental 486 difference in verifying the performance of our approach. 487

B. Enriching Low-Resolution Load Measurements

Fig. 8 shows one-day actual and enriched 1-second load 489 data for a service transformer. As can be seen, the enriched 490 curve can accurately follow the actual basic load pattern. Note 491 that our goal is not to force the enriched 1-second data to 492



Fig. 8. One-day actual and enriched 1-second load curves.



Fig. 9. The estimated maximum and minimum loads against the corresponding actual values.

⁴⁹³ exactly track the actual load. Instead, our method is designed ⁴⁹⁴ to restore the *statistical* properties of instantaneous load given ⁴⁹⁵ known low-resolution load observations obtained from hourly ⁴⁹⁶ SM data.

⁴⁹⁷ One critical step of our proposed approach is to determine ⁴⁹⁸ the masked maximum and minimum loads given a known ⁴⁹⁹ average load observation on an hourly basis. Thus, it is of ⁵⁰⁰ significance to examine the performance of the load boundary ⁵⁰¹ inference process. To do this, we have employed the coef-⁵⁰² ficient of determination, R^2 , for fitness evaluation, which is ⁵⁰³ defined as:

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$$R^{2} = 1 - \frac{\sum_{i=1}^{N} (y_{i} - \hat{y}_{i})^{2}}{\sum_{i=1}^{N} (y_{i} - \bar{y})^{2}},$$
(21)

)

 $_{505}$ where, y_i denotes the real maximum/minimum instanta-506 neous load, \hat{y}_i denotes the corresponding inferred maximum/minimum instantaneous load, and $\overline{y} = \frac{1}{N} \sum_{i=1}^{N} y_i$. Fig. 9 507 ⁵⁰⁸ illustrates the effectiveness of load boundary estimation, and 509 it can be seen that the estimated bound shows a linear rela-510 tionship with the actual bound. The R^2 values for the upper 511 and lower bounds are 0.80 and 0.83, respectively. This can 512 also corroborate the accuracy of our proposed method. To 513 fully evaluate the performance of our approach on load bound-514 ary inference, we have also computed relevant error metrics ⁵¹⁵ based on the high-resolution load in Fig. 8. The error metrics 516 include the absolute error (AE) and the root mean square error 517 (RMSE), and the results are summarized in Table I. The error 518 metrics demonstrate that our method can accurately recover 519 the unknown upper and lower bounds of the instantaneous 520 load.

 TABLE I

 Computed Error Metrics of Inferring Load Boundary



Fig. 10. Distributions of the actual and enriched 1-second load in Fig. 8.



Fig. 11. Percentiles of the actual and enriched 1-second loads in Fig. 8.

Note that our final goal is to recover the statistical prop- 521 erties of the high-resolution load within each low-resolution 522 sampling interval. Therefore, the performance of our proposed 523 approach needs to be evaluated from the perspective of statis- 524 tics. Fig. 10 illustrates the distributions of the actual and 525 enriched load samples on the load curves shown in Fig. 8. 526 It demonstrates that the enriched load distribution closely 527 matches the actual load distribution. In comparison, the non- 528 enriched load curve, which only includes 24 load observations, 529 cannot sufficiently form a satisfactory distribution. In addi- 530 tion, to quantitatively assess load enrichment performance, we 531 have examined the differences between the actual and enriched 532 load values corresponding to different percentiles, as shown 533 in Fig. 11. We have also evaluated the difference between 534 the percentiles of the enriched load and the actual load. The 535 computed maximum, minimum, median absolute errors of the 536 percentiles are 2.7, 0.31, and 1.5, respectively. The RMSE is 537 1.6. Therefore, the differences are small, which also proves 538 the effectiveness of our proposed approach from a statistical 539 perspective. 540

It is also of interest to examine the results obtained using our proposed load data enrichment framework with a *first* order Markov chain model. Fig. 12 presents the actual high resolution load curve and the enriched load curve based on a first-order Markov model. To assess the different effects of the first- and second-order Markov models on load vari ation inference, we have constructed the distributions of load state duration, as shown in Fig. 13, where, *D* denotes the load state duration. By comparing Figs. 13(b) and 13(c) with



Fig. 12. One-day actual and enriched 1-second load curves (1st-order Markov model).



Fig. 13. Distributions of load state duration corresponding to the actual load and the enriched loads.



Fig. 14. Percentiles of load state duration corresponding to the actual load and the enriched loads.

Fig. 13(a), respectively, we can see that Fig. 13(b) is more similar to Fig. 13(a) than Fig. 13(c). This means that our proposed method can recover the load variation with relatively higher fidelity compared with the method with a first-order Markov model. This can also be corroborated by Fig. 14, where, for the percentiles of load state duration corresponding to our proposed method are closer to the percentiles corresponding to the actual load.

558 C. Robustness to PV Integration

In modern distribution systems, PV integration is common 559 ⁵⁶⁰ for utilities. Therefore, it is necessary to test the performance of our load data enrichment approach under the condition 561 ⁵⁶² of PV integration. Specifically, three scenarios are considered where in all scenarios, both the teacher transformer and the 563 student transformer supply six customers. In the first scenario, 564 ⁵⁶⁵ three of the six customers supplied by the teacher transformer ⁵⁶⁶ have installed PVs, and the ratio of the peak PV generation the peak load of the teacher transformer is 44%. In the 567 to 568 second scenario, only the student transformer supplies three 569 PV-installed customers, and the ratio of the peak PV genera-570 tion to the peak load of the student transformer is 32%. In the 571 third scenario, the teacher and student transformers both have



Fig. 15. Robustness of our proposed approach to small-scale PVs.

three PV-installed customers, and the ratios of the peak PV 572 generation to the peak loads of the teacher and student trans- 573 formers are 40% and 34%, respectively. The enrichment results 574 corresponding to the three foregoing scenarios are shown in 575 Fig. 15. It is demonstrated that the proposed approach can still 576 achieve accurate high-resolution load data enrichment when 577 the teacher and/or student transformers serve PV-installed cus- 578 tomers. Quantitatively, for the first scenario, the maximum, 579 minimum, and median absolute errors between the percentiles 580 of the enriched load and the actual load are 1.91, 0.23, and 581 0.96, respectively. For the second scenario, the three computed 582 error metrics are 3.24, 1.85, and 2.40, respectively. For the 583 third scenario, the three computed error metrics are 3.24, 1.85, 584 and 2.40, respectively. In summary, the error metrics demon- 585 strate that our proposed load data enrichment framework can 586 adapt to PV integration. 587

D. Performing Time-Series Power Flow Studies

To thoroughly examine the performance of our proposed ⁵⁸⁹ approach, we have conducted time-series power flow studies ⁵⁹⁰ by separately feeding the actual and enriched loads into a real ⁵⁹¹ distribution system [18]. The one-line topology of the real distribution system is shown in Fig. 16. Bus voltages obtained ⁵⁹³ from power flow analysis, which are critical to distribution ⁵⁹⁴ system operators, are used to evaluate our proposed approach. ⁵⁹⁵ Specifically, we compare the distributions of bus voltages and ⁵⁹⁶ voltage ramps obtained from power flow studies based on the ⁵⁹⁷ actual and enriched high-resolution load data, respectively. The ⁵⁹⁸ reason for assessing voltage ramp is that voltage ramp is significant for renewable energy integration [8]. The voltage ramp

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Fig. 16. One-line diagram of a real distribution system.



Fig. 17. Distributions of voltage and voltage ramp during a certain hour interval for Bus 57.

 $_{601} \Delta V$ is defined as the difference between the current voltage $_{602}$ value and the last voltage value.

Fig. 17 illustrates the distributions of voltages and voltage 603 604 ramps during a certain hour interval for Bus 57 in the real 605 distribution system. In Fig. 17(a), it is observed that the empir-606 ical probability density function (PDF) of voltage based on the 607 actual high-resolution load data can closely fit that based on 608 the enriched high-resolution load data. For comparison, we 609 have also performed a *snapshot* flow study using the average 610 load over the same hour interval. The per-unit voltage for Bus 57 is 1.0124, which is a single value without statistical prop-611 612 erties. Therefore, the voltage distribution in Fig. 17(a) fully 613 proves the capability of our proposed approach for recovering 614 statistical characteristics masked by the low-resolution aver-615 age load measurements. This capability can further enhance 616 distribution system observability and situational awareness. A 617 similar conclusion can be drawn for the voltage ramp, whose 618 distribution is shown in Fig. 17(b). As can be seen, the two voltage ramp distributions corresponding to the real rich load 619 620 data and the enriched load data closely match each other. In 621 comparison, the single bus voltage value based on the hourly 622 average load cannot demonstrate probabilistic properties. It is 623 important to point out that voltage distribution also depends on 624 the specific structure of distribution systems in addition to spe-625 cific load observations. For example, if a distribution system 626 has very short line segments and a strong connection with a 627 transmission system, then the bus voltage deviation might not be significant. In contrast, for a weak grid-connected distri-629 bution system with long line segments, the loads can have a 630 strong impact on bus voltages.

E. Performance Comparison

It is of significance to compare our approach with other ⁶³² methods presented in previous works. We primarily focus on ⁶³³ comparing our approach with an allocation-based methodol- ⁶³⁴ ogy introduced in [8] and a noise-based technique presented ⁶³⁵ in [12], which are two primary load data enrichment ⁶³⁶ approaches in previous works. ⁶³⁷

1) Comparison With the Allocation-Based Method: The 638 allocation-based method involves two steps. First, a low- 639 resolution substation- or feeder-level load profile is scaled 640 to obtain service transformer-level load profiles, according 641 to transformer capacity or peak load. Then, the scaled low- 642 resolution load profile is enriched using a variability library, 643 which is constructed by applying the discrete wavelet trans- 644 form algorithm to known high-resolution transformer-level 645 load measurements. An alternative to scaling low-resolution 646 load profile is to obtain a load pattern obtained by scal- 647 ing known typical load profiles of other transformers, as 648 presented in [8]. For conciseness, we refer to the techniques 649 presented in [8] as the allocation-based method. The perfor- 650 mances of our approach and the allocation-based approach 651 are shown in Figs. 18(a) and 18(b), respectively, where the 652 actual and enriched load curves on a certain day are presented. 653 In Fig. 18(a), we can observe that the basic pattern of the 654 enriched 1-second load can flexibly follow the actual load 655 variation, despite load uncertainty. The superior performance 656 of our approach results from two aspects, the fine spatial gran- 657 ularity of SM data and the design of load boundary inference 658 process. In comparison, the allocation-based load enrichment 659 approach fails to accurately track the basic load pattern, as 660 demonstrated in Fig. 18(b). 661

The performance of the allocation-based method can also ⁶⁶² be evaluated by examining the R^2 values computed for the ⁶⁶³ load bounds, as shown in Fig. 19. We can observe that the ⁶⁶⁴ R^2 values are negative, which means that the estimated maximum/minimum bound offers a poor estimation of the variation ⁶⁶⁵ of the actual maximum/minimum bound. The unsatisfying ⁶⁶⁷ performance of the allocation-based approach can also be ⁶⁶⁸ viewed by observing the two scatter plots in Fig. 19, where, ⁶⁶⁹ most scatters are located above the upper-right diagonal line, ⁶⁷⁰ indicating an overestimation of the actual load bounds.

To further evaluate the performance of our approach and ⁶⁷² the benchmark methods, we have also computed the cumulative probability of the actual and enriched load presented ⁶⁷⁴ in Fig. 18. The empirical cumulative distribution functions ⁶⁷⁵ (ECDFs) are illustrated in Fig. 21, where, we can observe ⁶⁷⁶ that the ECDF corresponding to our method is much closer ⁶⁷⁷ to the ECDF of the actual load than the ECDF correspond-⁶⁷⁸ ing to the allocation-based method. To quantitatively assess ⁶⁷⁹ the similarity between the two ECDFs, we have computed ⁶⁸⁰ the two-sample Kolmogorov-Smirnov (KS) statistic for each ⁶⁸¹ method, using the following equation: ⁶⁸²

$$D = \sup_{P} |F_a(P) - F_e(P)|,$$
(22) 683

where, sup denotes the supremum of the set of distances. ⁶⁸⁴ $F_a(P)$ denotes the ECDF of the actual high-resolution load, ⁶⁸⁵ and $F_e(P)$ denotes the ECDF of the enriched load. Intuitively, ⁶⁸⁶

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(a) Actual curve and the enriched curve using our approach



(b) Actual curve and the enriched curve using an allocation-based approach



(c) Actual curve and the enriched curve using a noisebased approach

Fig. 18. The actual high-resolution load curve and the enriched load curves.



Fig. 19. The estimated maximum and minimum load bounds obtained from the allocation-based method against the corresponding actual values.

⁶⁸⁷ *D* measures the largest pairwise absolute distance between the ⁶⁸⁸ ECDFs of the actual load and the enriched load. In Fig. 21, we ⁶⁸⁹ can observe that the two-sample KS statistic for our method ⁶⁹⁰ is 0.14, which is significantly smaller than the statistic for the ⁶⁹¹ allocation-based method, which is 0.40.

2) Comparison With the Noise-Based Method: The basic 692 ⁶⁹³ idea of the noise-based approach is to add Gaussian noise to a ⁶⁹⁴ typical or known low-resolution load profile. Fig. 18(c) shows 695 the actual 1-second load curve and the enriched load curve 696 obtained by the noise-based approach. One primary shortcom-697 ing of the noise-based approach is that it can not faithfully 698 capture the cyclicity of the load state. This shortcoming can ⁶⁹⁹ be observed in Fig. 18(c), where, the enriched load curve clutters the plot and does not present a clear duration of load state. 700 The unsatisfactory performance of the noise-based approach 701 can also be corroborated by Fig. 20, where, the negative R^2 702 values demonstrate poor explanations of the inferred maxi-703 704 mum/minimum load bound on the actual load bound. The



Fig. 20. The estimated maximum and minimum load bounds obtained from the noise-based method against the corresponding actual values.



Fig. 21. Cumulative probability distributions of the actual load and the enriched load in Fig. 18.

 TABLE II

 COMPUTED ERROR METRICS BASED ON LOAD CURVES IN FIG. 18

	Our Approach	Allocation-based	Noise-based
nMAE (%)	12.3	22.8	21.9
nRMSE (%)	16.4	28.1	27.5

computed *D* value for the noise-based method is 0.32, which $_{705}$ is greater than 0.14, as shown in Fig. 21. This demonstrates $_{706}$ that our method has a better performance than the noise-based $_{707}$ method in terms of the two-sample KS statistic. $_{708}$

To quantitatively compare the aforementioned three 709 approaches, we have also computed the normalized mean 710 absolute error (nMAE) and the normalized root mean square 711 error (nRMSE) based on the load curves in Fig. 18. 712 Specifically, nMAE and nRMSE are computed as follows: 713

$$nMAE = \frac{\frac{\sum_{t=1}^{n_t} |P(t) - \hat{P}(t)|}{n_t}}{P_{max}} \times 100\%, \qquad (23) \quad 714$$

$$nRMSE = \frac{\sqrt{\frac{\sum_{t=1}^{n_t} (P(t) - \hat{P}(t))^2}{n_t}}}{P_{max}} \times 100\%, \qquad (24) \quad 715$$

where, n_t is the total number of samples in a day with a 716 resolution of 1 second, i.e., 86400. P(t) and $\hat{P}(t)$ denote 717 the actual and estimated loads at time *t*, respectively. P_{max} 718 denotes the peak of the actual load. The computed error met-719 rics are summarized into Table II. We can see that compared 720 to the allocation- and noised-based methods, our approach has 721 smaller errors.

This paper is devoted to temporally enriching low-resolution 724 load data for service transformers that only have SMs, using 725

726 high-resolution load data from service transformers with 727 micro-PMUs and SMs. The entire process includes two stages. 728 determining the maximum and minimum load bounds using known low-resolution load measurements and trained regres-729 sion models, and inferring load variability within load bound-730 aries using trained probabilistic transition models. The regres-731 sion and transition models are trained using high-resolution 732 load data from service transformers with micro-PMUs. We 733 have used real high-resolution load data to prove that our 734 735 approach is able to accurately recover high-resolution load data 736 masked by the average load measurements over low-resolution 737 sampling intervals. The enriched high-resolution load data can significantly enhance utilities' grid-edge observability and sit-738 739 uational awareness of distribution systems. Our paper's key 740 findings are summarized as follows.

- The 1-second load within an hourly interval can be 40%
- times larger or smaller than the corresponding average
- load during the same hour interval. By performing power
- flow studies, we have found that using the hourly average
- ⁷⁴⁵ load for conducting power flow analysis cannot accu-⁷⁴⁶ rately capture the actual condition of distribution systems.
- Therefore, performing low-resolution power flow studies
 might cause significant errors, especially for those distribution networks that have a weak grid connection and
 long line segments.
- The numerical experiments have verified that our proposed approach shows strong robustness and adaptability to PVs.
- The numerical experiments have also demonstrated that our approach can accurately recover statistical properties of the instantaneous load within each low-resolution sampling interval of SM. The power flow studies show that our approach can faithfully reflect distribution system's actual voltage conditions from a statistical perspective.

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