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Abstract—Repair and reconfiguration are vital for power recovery after outages caused by natural disasters in distribution systems, but sequential and uncertainty-inflicted decision points due to uncertain repair periods make power recovery complicated. This paper proposes semi-Markov decision process (SMDP)-based resilient recovery with sequentially event-driven repair and reconfiguration in consideration of uncertainty-inflicted decision-making points. The sequential repair/reconfiguration actions in consideration of uncertain repair periods are considered as uncertainty-inflicted event-driven processes. The sequential repair states with different repair crews are established as semi-Markov states. The whole sequential and uncertain decision-making process is modeled as a semi-Markov decision process-based optimization model, which is an event-driven recursive model. Q-learning is employed to solve the proposed model, and the convergent estimations of Q values for semi-Markov states map the original model into an event-driven deterministic optimization based on the sequential repairs that actually occurred over the time horizon. IEEE 123-bus system is used to validate the proposed model.

Index Terms—repair, resilient recovery, semi-Markov decision process, uncertain decision-making

NOMENCLATURE

Indices and Sets

e, e′
Index of semi-Markov states indicating different event e and e′.
i
Index of repair crews.
j
Index of damaged components.
l
Index of lines.
k, k′
Index of terminal buses of line l.
g
Index of optimization variables related to semi-Markov states.
A
Set of actions.
B
Set of power buses.

Set of substation nodes.

E
Set of semi-Markov states.

L
Set of lines.

L′
Set of dispatchable lines.

N′k,
Set of power buses connected to power bus k under semi-Markov state S′e.

Ωcr
Set of repair crews.

Ωfc
Set of damaged components.

Notations for semi-Markov Decision Process-based model

S′e, S′′e
Semi-Markov states.
ae
Actions for semi-Markov state S′e.
v,e,v′
Value functions for semi-Markov state S′e and S′′e.
C
Immediate cost with semi-Markov state S′e under action ae.
P
Probability from semi-Markov state S′e to S′′e under action ae.

ΔL′e
Loss of load with semi-Markov state S′e.

ΔL′′e
Loss of load with semi-Markov state S′′e on the (n + 1)th stochastic path.

η
Coefficient for load of repair.

τ
Start and end time for one event including the repair and the corresponding transportation.

Q′(S′e)
Q′′(S′′e)
Q value for semi-Markov state S′e.

Q′(S′e)
Q′′(S′′e)
Q value for semi-Markov state S′†e at the n′th iteration.

Q′′(S′′e)
Estimated Q value for semi-Markov state S′′e at the n′th iteration.

Parameters

η
Coefficient for loss of load.

C
Coefficient for operational cost, switch-on, and switch-off costs of lines.

Pmax, Qmax
Maximum active load and reactive load at bus k with semi-Markov state S′e.

rkk′, xkk′
Resistance/reactance of line k − k′.

γl,e
Given value representing failure state of line l with semi-Markov state S′e.

M
A large number.

Skk′
Apparent power capacity of line k − k′.

λ
A given value representing whether the component j is repaired.

Dynamic learning rate, and it is the mean value of slopes of Q value curves at the n′th iteration.
natural disasters, and the computational complexity of the investigated in [13] to restore multiple outages caused by mobile battery-carried vehicles and networked microgrids is faster post-disaster deployment of equipment resources and crews to damage locations. An integrated model scheduling of the [12] to preposition crews and equipment aiming to achieve as possible, there have been many research studies on system restoration, and one preprocessing approach, which cuts down the number of candidate nodes for connecting mobile power sources and preassigns a minimal set of repair crews to damage locations. An integrated model scheduling mobile battery-carried vehicles and networked microgrids is investigated in [13] to restore multiple outages caused by natural disasters, and the computational complexity of the proposed model is reduced by the auxiliary induction function-based approach. Based on multiple microgrid formulation, [14] proposes a hierarchical outage management scheme to deal with power outages, and [15] investigates a heuristic approach-based microgrid formulation to address computational intractability. When forming microgrids after power outages, distributed generators have great impacts on microgrid operation. [16] investigates dynamic characteristics of distributed generators, and the corresponding influences are integrated into the recovery model. During the distribution system recovery, radiality is one of important constraints and the single-commodity flow constraints are presented in [17] to address the limitation of spanning tree constraints. In consideration of the couplings between different systems, the poster recovery on the interdependent power and natural gas system is investigated in [18], and the coordinated recovery model for transmission and distribution systems is established in [19]. A new metric, defined as the number of recovered customers divided by the average outage time of the interrupted customers, is developed in [20] to evaluate the resilience enhancement strategies. With the development of intelligence algorithms, the optimal equipment repair sequence can be searched by means of the heuristic algorithm [21], and machine learning techniques can be used to train an agent with thousands of off-line scenarios to obtain the optimal recovery strategy [22]. In addition, communication systems in the cyber-physical system have also great impacts on power system resilience. A hierarchical two-stage robust optimization is investigated in [23] to mitigate the impacts of false data injection on the integration of electricity and gas systems, increasing the integrated system resilience. In consideration of emergency communication vehicles, an integrated recovery model coordinating physical systems and cyber systems is investigated to restore unserved load as soon as possible [24]. A two-stage sequential disaster recovery model is established in [25] to collaborate cyber-physical optimization.

To achieve a fast recover, repairs on damaged components are critical. In [26], the post-disaster repair repair process is established as a scheduling problem with a set of newly-defined soft precedence constraints, and a polynomial-time algorithm in consideration of constant performance guarantees is employed to solve the proposed model. In [27], the model of dispatching maintenance/restoration crews is integrated into the disaster recovery model that scheduling the action sequence for controllable switches and controllable load. In [28], a co-optimization model is investigated to schedule repair crews and mobile power sources in transportation networks and distribution systems in consideration of different timescales of distribution system restoration, and one preprocessing approach, which cuts down the number of candidate nodes for connecting mobile power sources and preassigns a minimal set of repair tasks to depots, is used to reduce computational complexity. In [29], a mixed-integer linear programming model is constructed to co-optimize repair crews and resources to restore unserved loads after power outages caused by natural disasters, and an iterative neighborhood search approach is used to solve the proposed model.

In the real world, the repairs on the damaged components depend on many factors, e.g., transportation conditions, damage conditions, and external environment. Theses factors result in uncertain periods of sequential repairs, and uncertain repair periods cause a consequence that the repair decisions cannot be made at the specified and fixed time. This kind of

Variables

\[ x_{le}, x_{le}’ \]

Binary variables representing on-off states of line \( l \) under semi-Markov state \( S_e \) and \( S_e’ \), respectively. 1 denotes on state, and 0 denotes off state.

\[ x_{le}’, x_{le}” \]

Binary variables representing switch-on and switch-off actions, respectively.

\[ y_{ij’e} \]

Binary variables representing the repair state of the \( j \)th damaged component with the \( i \)th repair crew.

\[ o_{kk’e} \]

Binary variables, the value is 1 if bus \( k’ \) is the parent bus of bus \( k \) with semi-Markov state \( S_e \).

\[ P_{ke}, Q_{ke} \]

Active load and reactive load at bus \( k \) with semi-Markov state \( S_e \).

\[ P_{kk’e}, Q_{kk’e} \]

Active and reactive power through line \( k-k’ \) with semi-Markov state \( S_e \).

\[ U_{ke} \]

Squared voltage magnitude of bus \( k \) with semi-Markov state \( S_e \).

\[ \beta_{ge} \]

Semi-Markov state-related variables including \( x_{le}’, \forall l \) and \( y_{ij’e}, \forall i,j \).

\[ \varsigma_{ge} \]

Variables related to \( \beta_{ge} \).

I. INTRODUCTION

COMMERCIAL and residential customers are directly connected to radial distribution systems, and any failures due to damaged components caused by natural disasters or cyber attacks will result in massive loss of loads [1]. Many organizations, e.g., the North American Electric Reliability Corporation [2] and the United States Electric Power Research Institute [3], have released reports emphasizing that energy systems should have characteristics of resilience against natural disasters or cyber attacks. As suggested, many preventive and adaptive strategies are investigated to improve power system resilience from the perspectives of network hardening [4], unfolding strategies [5], and cyber security [6]. For example, a two-stage stochastic mixed integer model, in which the first stage aims to obtain the optimal hardening scheme and the second stage includes the potential damages, is investigated in [4] to improve the resilience against extreme weather events. In [7], a state-based decision-making model is proposed to increase system resilience with the objective of minimizing loss of loads during an unfolding sequential event. In [8], a two-step optimization model in consideration of predisaster preparedness and post-disaster resource re-allocation is constructed to improve distribution system resilience.

Although many existing preventive and adaptive strategies are investigated to improve power system resilience [9], damaged components caused by natural disasters are inevitable and in consequence power outages due to damaged components are also unavoidable. To achieve system recovery as quickly as possible, there have been many research studies on system recovery from the perspectives of system reconfiguration [10], microgrid formulation [11], etc. For example, a stochastic optimization model for resource preparation is investigated in [12] to preposition crews and equipment aiming to achieve faster post-disaster deployment of equipment resources and crews to damage locations. An integrated model scheduling mobile battery-carried vehicles and networked microgrids is investigated in [13] to restore multiple outages caused by natural disasters, and the computational complexity of the
decision-making process at uncertain decision time points due to uncertain sequential repairs is different from the decision-making process at the given decision time points, and needs to be investigated. The semi-Markov decision process is an effective framework for the sequential decision-making process at uncertain decision time points. Currently, the semi-Markov decision process has been used in maintenance scheduling [30], reliability evaluation [31], availability analysis [32], etc. In [33], a semi-Markov decision process-based optimization model, estimating conditional reliability under varying conditions, is established to obtain the maintenance scheme. In consideration of random holding time of system states, [34] investigates power-plant reliability analysis by means of semi-Markov processes. With the massive deployment of cyber technologies, the semi-Markov models represent the intrusion process of measurement manipulation [35] and penetration attacks [36] to evaluate power system reliability. The semi-Markov decision process has not been used in system recovery in consideration of the decision-making process at uncertain decision time points. Therefore, a semi-Markov decision process (SMDP)-based resilient recovery model is proposed to investigate the decision-making process at uncertain decision time points due to uncertain sequential repairs. The contributions of the paper are listed as follows. 1) An uncertainty-inflicted event-driven process is used to describe sequential repair/reconfiguration problem in consideration of uncertain decision points due to uncertain repair periods. 2) The uncertainty-inflicted event-driven process is established as a semi-Markov decision process-based model, which is an event-driven recursive model. 3) To address the dimensionality curse of the problem, Q-learning with the dynamic learning rate is used to estimate the expected values of semi-Markov states by means of off-line iterations, and the converged estimations of Q values for semi-Markov states map the original model into an event-driven deterministic optimization. IEEE 123-bus system is used to validate the proposed model, and the results show that the proposed model and the algorithm have a good performance on sequentially event-driven repair/reconfiguration in consideration of uncertainty-inflicted decision-making points.

The remainder of this paper is organized as follows. Section II shows the uncertainty-inflicted event-driven process. Section III presents the semi-Markov decision process-based event-driven optimization, and section IV introduces Q-learning solution and model reformulation. The case studies and the conclusions are demonstrated in Section V and Section VI.

II. UNCERTAINTY-INFLECTED EVENT-DRIVEN PROCESS

A. Description of Uncertainty-Inflicted Event-Driven Process

In the real world, many events occur sequentially one by one after given actions and the duration of each event is uncertain. In this case, the decision time point of each action is also uncertain. This kind of decision-making process at uncertain decision time points due to uncertain sequential events, different from the decision-making process at the given decision time points, is defined as an uncertainty-inflicted event-driven process in our study. Take the repair action in the distribution system as an example. After component failures caused by natural disasters in the distribution system, system repair needs to recover the system to the normal state as quickly as possible. Due to limits of repair resources and system operational constraints, system repair is a sequential process. In addition, component repair depends on transportation conditions, damage conditions, external environment, etc. These make component repair time uncertain, making each repair become an uncertain event. Because repairs on different failure components are implemented sequentially, uncertain repair periods and sequential implementation make the entire recovery become an uncertainty-inflicted event-driven process.

Take the recovery process in Fig. 1 as an example. The lines 1-2, 3-4, 6-7, and 9-10 are in failure due to natural disasters, and in consequence power load at the buses 2, 3, 4, 5, 6, 7, 8, and 9 are disconnected. The line 7-9 has a switch for system reconfiguration. To recover the system and reduce the loss of loads, the following recovery processes can be implemented.

- **Process 1**: Dispatch Crew 1 to repair the lines 6-7 (the repair ) and 3-4 (the repair ) sequentially. Dispatch Crew 2 to repair the line 9-10 (the repair ), and meanwhile connect the line 7-9 by means of the switch.

- **Process 2**: Dispatch Crew 1 to repair the line 6-7 (the repair ) and 3-4 (the repair ) sequentially, and meanwhile connect the line 7-9 by the switch.

For the above two recovery processes, the repair is implemented after the repair implemented by the crew or the repair implemented by the crew 2. Due to uncertain repair periods, it is not sure that which of and is first completed due to sequential characteristics. If the repair is first completed, we could implement Process 1. If the repair is first completed, we could implement Process 2. So, it indicates that the implementation of the repair depends on the previous uncertain event, and we define this as an uncertainty-inflicted event-driven process. This also demonstrates that an optimal strategy needs to be made based on observed repairs that actually occurred. In this study, the semi-Markov decision process is employed to describe and model the uncertainty-inflicted event-driven process.

![Fig. 1. Uncertainty-inflicted event-driven process.](image-url)
B. Modeling of Uncertainty-Inflicted Event-Driven Process

Fig. 2 shows the time horizon for the uncertainty-inflicted event-driven process. In Fig. 2 (a), \( r_1 \) denotes the time period to repair the line 6-7, and \( d_1 \) is the time period to route the crew 1 to the location of the line 6-7. We define the state in this period as a state \( r_{11}^D \), as shown in Fig. 2 (b). During the state \( r_{11}^D \), the crew 1 cannot be re-dispatched. Only when the repair is finished, the crew 1 can be re-dispatched again. Due to uncertain repair periods, the decision points for re-dispatching crews are event-based and uncertain. When there are multiple groups of crews, the scenarios will become more complicated. The decision points of the system are Cartesian products of each decision point of different crews in consideration of their uncertain repair periods and sequential interdependence. For example, decisions should be made in the state \( \{r_{11}^E, r_{23}^D, \Pi_e\} \) and \( \{r_{12}^D, r_{23}^E, \Pi_e\} \). The superscript ‘\( D \)’ denotes ‘during one scheduled action’, indicating no other actions can be implemented by the corresponding crew, and the superscript ‘\( E \)’ denotes ‘the scheduled action is completed’, indicating new actions can be implemented by the corresponding crew. \( \Pi_t \) represents the system topology at time \( t \). \( r_{11}^E \) denotes that the repair implemented by the first crew on the 1st failure component is finished. \( r_{33}^D \) denotes the 3rd failure component is being repaired by the second crew. \( r_{12}^D \) denotes that the 2nd failure component is being repaired by the first crew . \( r_{23}^E \) denotes the repair implemented by the second crew on the 3rd failure component is finished.

The semi-Markov decision process (SMDP) can be expressed as a four-tuple \((S, A, P, R)\), in which \( S \) and \( A \) represent the semi-Markov state space and the action space, respectively. \( P \) is the transition probability after actions under a state. \( R \) is the reward after actions. A semi-Markov decision process is an extension of a Markov decision process that includes an agent that makes decisions that affect the evolution of the system over time. For the semi-Markov decision process, one critical difference from the Markov decision process is that the duration of each state is stochastic. Fig. 3 illustrates the semi-Markov decision process. When observing the state \( S_t \), one action \( A_t \) is performed, resulting a reward \( R_t \). After a stochastic duration \( T_t \), the state \( S_t \) reaches the \( S_{t+1} \) with the probability \( P_{t+1} \) in consideration of environment uncertainties. Then, this process is repeated for other decision points. The investigated uncertainty-inflicted event-driven process can be mapped into a semi-Markov decision process as follows.

- \( S \): The semi-Markov states include the system topology and the repair state for each group of crews. Each group of crews is dispatched as a whole, and there may be several groups who can be dispatched simultaneously.
- \( A \): The actions include repair dispatch and system reconfiguration by means of controlling line switches. It is assumed that the implementation time of controlling line switches is ignored, and system reconfiguration will be implemented at the initial time or the time when one failure component is repaired. Repair dispatch can only be implemented when the corresponding crews are unoccupied.
- \( P \): After re-dispatching the crews and implementing system reconfiguration, the next state is deterministic. This indicates that the transition probability from one state to another state with actions is 1.
- \( R \): The reward includes a discrete state-action dependent reward and a time-continuous reward with regard to uncertain repair time periods and future states.

The semi-Markov state \( S_e \) for the whole decision process can be expressed as follows.

\[
S_e = (s_{1e}, \ldots, s_{ie}, \ldots, s_{fe}, \Pi_e, \mathcal{L}_e) \quad \forall t \tag{1}
\]

where \( S_e \) represents the system state, \( \Pi_e \) is the state of the system topology in the system state \( S_e \), \( \mathcal{L}_e \) denotes the system load level in the system state \( S_e \). \( s_{ie} \) in (1) denotes the state of the i-th crew in the system state \( S_e \), and it can be expressed as follows.

\[
s_{ie} \in \{r_{11}^D, r_{12}^E, \ldots, r_{ij}^D, r_{ij}^E\} \quad \forall i \in \Omega_{cr}, j \in \Omega_{fc} \tag{2}
\]

where \( r_{ij}^D \) denotes that the j-th failure component is being repaired by the i-th crew. \( r_{ij}^E \) denotes that the repair implemented by the i-th crew on the j-th failure component is finished.
It is assumed that the load at each bus is considered as a block and the load at one bus would be connected to the grid when the power supply path is effective. This indicates that one system topology scenario has the corresponding supplied load level when having one given loading factor. Take the scenario in Fig. 2 as an example. If the connected line set is \[\{1-11, 11-10\}\], the loads at the buses 1, 11, and 10 will be connected to the grid, and the loads at these three buses cannot be partially dispatched. If the connected line set is \[\{1-11, 11-10, 1-2, 2-3, 2-6\}\], the loads at the buses 1, 10, 11, 2, 3, and 6 will be connected to the grid. However, different loading factors over the time horizon result in different power load even for the same system topology. Therefore, the system load level \(L_c\) in the semi-Markov state \(S_c\) is used to represent different loading factors. Because the loading factor is a continuous function with regard to time, the uncertain period of each repair corresponds to a continuous load level, resulting in infinite continuous states, as shown in Fig. 4 (a). The infinite continuous states make the problem difficult to be solved, so discrete states of the load level as shown Fig. 4 (b) are deployed in this study. The time step of discretizing the load level can be set to be 15 minutes or 30 minutes. The value of discretizing the load level can be set as the average value of load in each interval.

![Fig. 4](image.png)

Fig. 4. (a) Infinite continuous state and (b) finite discrete state of load level under uncertain periods of different repairs.

III. SEMI-MARKOV DECISION PROCESS-BASED EVENT-DRIVEN OPTIMIZATION

A. Event-Driven Recursive Model for Semi-Markov States

Section II clarifies that the entire decision process of repair and reconfiguration is uncertainty-inflected and event-driven. Due to the event-driven characteristics, it is expected to construct an event-driven rather than time-driven optimization as follows.

\[
v_c(S_c) = \arg \min_{a_c \in A} \left\{ C_c(S_c, a_c) + \sum_{e \in S_c'} P_{c'e}^{a_c} \left[ \int_{\tau_1}^{\tau_2} (\eta \cdot \Delta L_c)dt + v_{c'}(S_{c'}) \right] \right\}
\]

(3)

where \(v_c(S_c)\) and \(v_{c'}(S_{c'})\) represent the expected total rewards for the semi-Markov states \(S_c\) and \(S_{c'}\), and \(S_{c'}\) is the triggered state after the semi-Markov state \(S_c\) under the action \(a_c\). This indicates the event-driven process. \(P_{c'e}^{a_c}\) indicates the transition probability from one state to another state under one action. Here, ‘one state’ represents that the system is being repaired. Once one repair is finished, the next state is deterministic after re-dispatching the crews. This indicates that the transition probability from one state to another state under one action is 1, i.e., the value of \(P_{c'e}^{a_c}\) is 1. \(\tau_1\) and \(\tau_2\) are the beginning and ending times of the semi-Markov states \(S_{c'}\), and these two times are uncertain over the time horizon. The uncertain times indicate the sequential interdependence and uncertain repair time periods. Therefore, the optimization objective (3) can be rewritten as follows.

\[
v_c(S_c) = \arg \min_{a_c \in A} \left\{ C_c(S_c, a_c) + \left[ \int_{\tau_1}^{\tau_2} (\eta \cdot \Delta L_c)dt + v_{c'}(S_{c'}) \right] \right\}
\]

(4)

where the integral term \(\int_{\tau_1}^{\tau_2} (\eta \cdot \Delta L_c)dt\) represents the cost of loss of loads. Due to uncertain times, the cost of loss of loads is uncertain, and this leads to difficulties in solving the optimization model. The function \(C_c(S_c, a_c)\) represents the immediate cost when implementing the action \(a_c\) in the semi-Markov state \(S_c\), and this cost includes the operational cost of dispatchable lines and the cost for line switching. It can be expressed as follows.

\[
C_c(S_c, a_c) = \sum_{l \in E_c} (c_l \cdot x_{le} + c_l' \cdot x_{le}' + c_l'' \cdot x_{le}''')
\]

(5)

where the first term is the operational cost of dispatchable lines, the second and the third terms represent the costs of connecting and disconnecting dispatchable lines.

B. Operational Constraints for Semi-Markov States

When the system reaches \(S_{c'}\) after the action \(a_c\), the system operational constraints, e.g., radiality for non-islanding buses, power flow, power balance, line capability, and voltage limits, should be satisfied.

1) Radiality constraint: The distribution system needs to operate in a radial topology. Because some components, e.g., distribution lines, are in failure caused by extreme events, some buses may be in island states and these islanded buses cannot be connected to the grid before the fault components are repaired. In consideration of fault components and system reconfiguration, the spanning tree constraints are used to guarantee the network radiality.

\[
x_{le} = o_{kk'e} + o_{kk'e}\quad l = (k, k') \in L, e \in E
\]

(6a)

\[
\sum_{k' \in N_{k'e}} o_{kk'e} = 1 \quad k \in B, e \in E
\]

(6b)

\[
o_{kk'e} = 0 \quad k \in B, k' \in N_{k'e}, e \in E
\]

(6c)

\[
P_{kk'e} = 0 \quad (k, k') \in \Omega_{fc}, e \in E
\]

(6d)

\[
o_{kk'e} = 0 \quad (k, k') \in \Omega_{fc}, e \in E
\]

(6e)

where (6a) and (6b) show that two terminals of one connected distribution line have one parent bus under the semi-Markov state \(S_c\). In practice, the bus connected to the external system or the substation bus has no parent bus, and this is constrained by (6c). In addition, the directed multicommodity flow-based models of the spanning tree constraints [37] are used as supplementary constraints to ensure system radiality.

Because the loads connected to islanded buses cannot be supplied by power source, (6a)-(6c) cannot include this scenario. We use the constraint (6d) to represent the island scenario. The constraints (6d) and (6e) denote that the power flows through the fault lines are set to be 0.
2) **Line switching constraints**: From one semi-Markov state to another semi-Markov state, the following constraints regarding line switching need to be satisfied.

\[
\begin{align*}
    x_{le} & \geq x_{le'} - x_{le} & (7a) \\
    x_{le}' & \leq x_{le} & (7b) \\
    x_{le}'' & \leq 1 - x_{le} & (7c) \\
    x_{le}'' & \geq x_{le} - x_{le}' & (7d) \\
    x_{le}' & \leq 1 - x_{le}' & (7e) \\
    x_{le} & \leq x_{le}' & (7f)
\end{align*}
\]

where (7a)-(7c) represent the switch-on constraints, and (7d)-(7f) represent the switch-off constraints.

3) **Power balance constraint**: For each semi-Markov state, the in-flow and out-flow of each bus should be equal.

\[
\begin{align*}
    P_{ke} + \sum_{k' \in K_{ke}} P_{kk'e} &= 0 \quad k \in B, e \in E \quad (8a) \\
    Q_{ke} + \sum_{k' \in K_{ke}} Q_{kk'e} &= 0 \quad k \in B, e \in E \quad (8b) \\
    0 & \leq P_{ke} \leq P_{ke}^{\text{max}} \quad k \in B, e \in E \quad (8c) \\
    0 & \leq Q_{ke} \leq Q_{ke}^{\text{max}} \quad k \in B, e \in E \quad (8d) \\
    \Delta L_e &= \sum_k (P_{ke}^{\text{max}} - P_{ke}) \quad e \in E \quad (8e)
\end{align*}
\]

where (8a) and (8b) represent real power balance and reactive power balance, respectively. Because (6d) and (6e) constrain the power flow through the fault lines as 0, it indicates that the loads at the islanded buses are disconnected. (8c), (8d), and (8e) are the load constraints at bus \( k \) with the semi-Markov state \( S_e \).

4) **Power flow constraint**: For each semi-Markov state, the power flow through each line is a function with regard to terminal bus voltages of each line. Distflow is used to describe this expression as follows.

\[
\begin{align*}
    U_{ke} - U_{ke}' & \leq (2 - x_{le} - \gamma_{le} \cdot M + 2(r_{kk'} \cdot P_{kk'e} + x_{kk'} \cdot Q_{kk'e}) \quad l = (k, k') \in L, e \in E \quad (9a) \\
    U_{ke} - U_{ke}' & \geq (\gamma_{le} - x_{le} - 2) \cdot M + 2(r_{kk'} \cdot P_{kk'e} + x_{kk'} \cdot Q_{kk'}) \quad l = (k, k') \in L, e \in E \quad (9b)
\end{align*}
\]

where (9a) and (9b) are the DistFlow model [38], and the quadratic terms are ignored. \( \gamma_{le} \) denotes the failure state of the line \( l \), and it is a known parameter for the semi-Markov state \( S_e \). \( \gamma_{le} = 0 \) means that the line \( l \) is in failure due to extreme events, and \( \gamma_{le} = 1 \) means that the line \( l \) is in normal state. A sufficiently large \( M \) makes (9a)-(9b) redundant when the lines are in failure or disconnected. Associated with (6), (8) and (9), non-islanded buses with the radiality constraint and islanded buses are both included in the model.

5) **Line capacity constraint**: The power flow through each line should be within the limits in each semi-Markov state.

\[
\begin{align*}
    (P_{kk'e})^2 + (Q_{kk'e})^2 & \leq x_{le} \cdot \gamma_{le} \cdot (S_{kk'})^2 \\
    l = (k, k') & \in L, e \in E
\end{align*}
\]

where \( \gamma_{le} \) is a known parameter for the semi-Markov state \( S_e \). Due to the power and reactive power, (10) is a nonlinear constraint. A relaxed expression is used as follows.

\[
\begin{align*}
    -x_{le} \cdot \gamma_{le} \cdot S_{kk'} & \leq P_{kk'e} \leq x_{le} \cdot \gamma_{le} \cdot S_{kk'} \quad \forall l, e \quad (11a) \\
    -x_{le} \cdot \gamma_{le} \cdot S_{kk'} & \leq Q_{kk'e} \leq x_{le} \cdot \gamma_{le} \cdot S_{kk'} \quad \forall l, e \quad (11b) \\
    -\sqrt{2}x_{le} \cdot \gamma_{le} \cdot S_{kk'} & \leq P_{kk'e} + Q_{kk'e} \leq \sqrt{2}x_{le} \cdot \gamma_{le} \cdot S_{kk'} \quad \forall l, e \quad (11c) \\
    -\sqrt{2}x_{le} \cdot \gamma_{le} \cdot S_{kk'} & \leq P_{kk'e} - Q_{kk'e} \leq \sqrt{2}x_{le} \cdot \gamma_{le} \cdot S_{kk'} \quad \forall l, e
\end{align*}
\]

where the above constraints are linear inequality constraints because \( \gamma_{le} \) is a known parameter for the semi-Markov state \( S_e \).

6) **Voltage constraint**: The voltage limits should be satisfied when having the semi-Markov state \( S_e \).

\[
\begin{align*}
    V_k^2 & \leq U_{ke} \leq V_k^2 \\
    k & \in B, e \in E \quad (12)
\end{align*}
\]

where (12) limits the upper and lower voltage bounds of each bus at each semi-Markov state.

IV. Q-LEARNING SOLUTION AND MODEL REFORMULATION

This section first presents the difficulty in solving the proposed model, and then introduces how to use Q-learning approach to solve the model. Third, model reformulation with regard to semi-Markov states and optimization variables in consideration of Q-learning approach is presented, and finally the solution process is introduced.

A. **Difficulty of Model Solution**

There are three difficulties in solving the proposed model, and they are listed as follows.

- **Recursive optimization model**: The optimization model (4) shows that it is a recursive model with regard to different semi-Markov states. The recursive model represents the sequential characteristics of different semi-Markov states under different actions. A large number of semi-Markov states and actions result in curse of dimensionality.

- **Uncertainty-inflicted event-driven process**: In (4), \( \tau_1 \) and \( \tau_2 \) are the beginning and ending times of the semi-Markov states \( S_e \). These two times are uncertain, and they are related to sequential repairs and the uncertain time periods of repairs over the time horizon.

- **Implicit functions between semi-Markov states and optimization variables**: The optimization objective (4) is a function of the semi-Markov states \( S_e \) and \( S_{e'} \). However, the operational constraints are the functions with regard to optimization variables, e.g., line states and physical variables of power flow. The semi-Markov states cannot be directly mapped to the optimization variables.

The above three challenges make the proposed semi-Markov decision process-based optimization difficult to be solved. In consideration of the recursive characteristics with uncertainties caused by the semi-Markov decision process-based optimization, Bellman’s principle of optimality [39] indicates that the future cost can be estimated by a replacement value. Therefore, the Q-learning approach is used to address the first and the second challenges. In addition, a model reformulation approach is employed to address the third challenge.
B. Q-learning Approach

One critical point of the proposed model is to make decision based on the event-driven semi-Markov state. When having the semi-Markov state $S_e$, the value of the subsequent semi-Markov state $S_{e'}$ and the uncertain repair period $\tau_2-\tau_1$ make the model difficult to be solved. Q-learning is an approach that uses an optimal estimation $Q^*(S_{e'})$ to replace the uncertain and sequential terms, e.g., we have the following equation.

$$Q^*(S_{e'}) = \int_{\tau_1}^{\tau_2} (\eta \cdot \Delta L_c) dt + v_e(S_{e'})$$  \hspace{1cm} \text{(13)}$$

Based on (13), the optimization objective (4) can be rewritten as follows.

$$v_e(S_e) = \arg \min_{a_e \in A} \{C_e(S_e, a_e) + Q^*(S_e)\} \quad \forall e$$  \hspace{1cm} \text{(14)}$$

where $S_e$ is the resulting semi-Markov state from the semi-Markov state $S_{e'}$ under the action $a_e$. If we know the value of $Q^*(S_{e'})$ for different actions $a_e$, the optimal strategy for the semi-Markov state $S_{e'}$ can be easily solved subject to with the constraints (6)-(12).

The value of $Q^*(S_{e'})$ cannot be obtained directly due to the uncertainty caused by $\tau_1$ and $\tau_2$. The critical point for the Q-learning approach is to estimate the value of $Q^*(S_{e'})$ via off-line value iteration with stochastic paths by means of monte carlo sampling. To represent the iteration, the superscripts $n$ and $n+1$ are added in the model.

$$v_n^{n+1}(S_e) = \arg \min_{a_e \in A} \{C_e(S_e, a_e) + Q_n^{n+1}(S_{e'})\}$$  \hspace{1cm} \text{(15)}$$

$$Q^{n+1}(S_{e'}) = \exp(-\lambda) \cdot Q^{n}(S_{e'}) + (1 - \exp(-\lambda)) \cdot \left( \int_{\tau_1^{n+1}}^{\tau_2^{n+1}} (\eta \cdot \Delta L_c) dt + v_n^{n}(S_{e'}) \right)$$  \hspace{1cm} \text{(16)}$$

where the optimization objective (15) constrained by (6)-(12) with the known value of $Q_n^{n}(S_{e'})$ at the $(n+1)^{th}$ iteration. Then, the value of $Q^{n+1}(S_{e'})$ at the $(n+1)^{th}$ iteration is updated by means of (16). There are two updated dimensions in (16). The first dimension is the estimation of the corresponding semi-Markov state at the $(n)^{th}$ iteration, i.e., the term I on the right side of (16). The second dimension is the value of resulting semi-Markov state under the action at the $(n+1)^{th}$ iteration, i.e., the term II on the right side of (16). The value of $\tau_2^{n+1} - \tau_1^{n+1}$ is the uncertain repair time, which is generated by monte carlo sampling.

The parameter $\lambda$ is interpreted as the dynamic learning rate, and its value is the mean value of slopes of $Q$ value curves at each iteration. When the slope of the $Q$ value curve tends to be 0, i.e., the value of $\exp(-\lambda)$ tends to be 1, the left side of (16) tends to be the term I. This indicates that the $Q$ value is converged. Otherwise, the slope of the $Q$ value curve is not 0. In this case, the estimated values at the previous iteration, i.e., the term I in (16), and the resulting values under uncertainty at the current iteration, i.e., the term II in (16), are employed to updated the estimated values until $Q$ values are converged. With enough off-line iterations, the converged value of $Q^*(S_{e'})$ can be obtained, and online optimization can be implemented based on event-driven semi-Markov states by utilizing (14).

C. Model Reformulation

The Q-learning approach provides a good solving process for the proposed semi-Markov decision process-based event-driven optimization model. However, there is still one challenge in the solving process, i.e., the semi-Markov states are not explicit functions with regard to optimization variables such as line states. The non-explicit functions cause the difficulty in solving the optimization objective (15) constrained by (6)-(12). For a semi-Markov state, repair states and system topology states are related to actions, and the system loading factor is independent on actions. Therefore, additional variables, mapping repair states and system topology states, need to be included in the model.

1) Semi-Markov State Mapping Constraints: For (15) at the $(n+1)^{th}$ iteration, $C_e(S_e, a_e)$ can be represented as an explicit function with regard to optimization variables but $Q^{n+1}(S_{e'})$ cannot be represented as an explicit function with regard to optimization variables. The semi-Markov state $S_{e'}$ is related to line states and repair states, and in consequence (15) can be expressed as follows.

$$\min \left\{ \sum_{l} \left( c_l \cdot x_{1e} + c_l' \cdot x_{1e} + c_l'' \cdot x_{3e} \right) + \sum_{g} \left( \prod_{g} (2b_{ge} - 1) (\beta_{ge} + b_{ge} - 1) Q_{g}^{n} \right) \right\}$$  \hspace{1cm} \text{(17)}$$

where $Q_{g}^{n}$ is the estimated $Q$ value of the semi-Markov state $S_{e'}$ at the $n^{th}$ iteration and its value is given. $b_{ge}$ is the $(g,e)^{th}$ element in the matrix $b$ that is binary-coded to represent the relations between semi-Markov states and line/repair states, and $\beta_{ge}$ is a given value. The term $\prod_{g} ((2b_{ge} - 1) (\beta_{ge} + b_{ge} - 1))$ has the multilinear function, and a recursive McCormick envelope is used to transform the multilinear function into a group of linear inequality constraints. For the multilinear function $\beta_{1e} \cdot \beta_{2e} \cdot \beta_{ge}$, we introduce new additional variables listed in (18).

$$\begin{array}{ll}
\varsigma_{2e} = \beta_{1e} \cdot \beta_{2e} \\
\varsigma_{3e} = \varsigma_{2e} \cdot \beta_{3e} \\
\ldots \\
\varsigma_{ge} = \varsigma_{(g-1)e} \cdot \beta_{ge} \\
\end{array}$$  \hspace{1cm} \text{(18)}$$

Based on the new variables $\varsigma_{2e}, \varsigma_{3e}, \ldots, \varsigma_{ge}$, the multilinear function $\beta_{1e} \cdot \beta_{2e} \cdot \beta_{ge}$ can be transformed into a group of linear inequality constraints as follows.

$$\begin{array}{ll}
\varsigma_{2e} \leq \beta_{1e} \\
\varsigma_{2e} \geq \beta_{2e} + \beta_{3e} - 1 \\
\varsigma_{ge} \leq \beta_{ge} (g = 2, \ldots, m) \\
\varsigma_{ge} \geq 0 (g = 2, \ldots, m) \\
\varsigma_{ge} \leq \varsigma_{(g-1)e} \cdot \beta_{ge} (g = 3, \ldots, m) \\
\varsigma_{ge} \geq \beta_{ge} + \varsigma_{(g-1)e} - 1 (g = 3, \ldots, m) \\
\end{array}$$  \hspace{1cm} \text{(19)}$$

where the linear inequality constraints (19) based on the recursive McCormick envelope are equivalent to the original constraints (18) because $\varsigma_{2e}, \varsigma_{3e}, \ldots, \varsigma_{ge}, \beta_{1e}, \beta_{2e}, \ldots, \beta_{ge}$ are binary variables.

2) Repair Mapping Constraints: Before each event-driven repair, the repaired components that are not in the repair waiting listing will not be notified to the repair crews, and the repairs in the semi-Markov state $S_{e'}$ have the following constraints.

$$\kappa_j + \sum_{i} y_{j,i e} \leq 1 \quad \forall j$$  \hspace{1cm} \text{(20)}$$
\[ \sum_{j} y_{ij} e' \leq 1 \quad \forall i \]  \hspace{1cm} (21)

where \( \kappa_j \) is a given parameter representing whether the component \( j \) is repaired. If the component \( j \) is repaired, \( \kappa_j = 1 \); otherwise, \( \kappa_j = 0 \). (20) shows that unrepaired components can be scheduled to one repair crew. (21) indicates that one repair crew can only select one unrepaired component at the same time.

D. Q-learning Iteration

Based on (15), (16) and given \( Q \) values for semi-Markov states, the optimization model can be solved easily. \( Q \) learning utilizes a large amount of off-line iterative optimization and learning to achieve the convergent estimated \( Q \) values for semi-Markov states. The learning for \( Q \)-learning iteration is listed in Algorithm 1.

**Algorithm 1 Q-learning Iteration**

1: Step 1: Set the iteration counter \( n = 1 \) and the maximum number of iterations \( N \), respectively.
2: Step 2: Set the initial value of \( Q_e^n \) for each semi-Markov state \( S_i' \) as 0.
3: Step 3: Do until all damaged components are repaired.
   4: \hspace{0.5cm} Step 3.1: Optimize the following model.
   5: \hspace{1cm} \textit{Obj.} \hspace{0.5cm} (17)
   6: \hspace{1cm} s.t. \hspace{0.5cm} (6) \hspace{-0.2cm} - \hspace{-0.2cm} (12), (18) \hspace{0.2cm} - \hspace{0.2cm} (21)
   7: \hspace{1cm} Step 3.2: With the optimization in Step 3.1, the optimal event-driven strategy (repair and reconfiguration) for the semi-Markov state can be determined. Generate the stochastic repair period \( \tau_2 = \tau_1 \) on the stochastic paths.
   8: \hspace{0.5cm} Step 3.3: Use (16) to update the \( Q \) value of the corresponding semi-Markov state at the \( (n+1) \)th iteration.
   9: \hspace{0.5cm} Step 3.4: With the repair periods for all crews repairing components, determine the next event-driven state and repeat Step 3.1 until all damaged components are repaired.
10: Step 4: Set \( n=n+1 \). If \( n \leq N \) go to Step 3.
11: Step 5: If \( n = N \), return the estimated \( Q \) values for semi-Markov states.

V. CASE STUDIES

In this section, a revised IEEE 123-bus system is used to verify the proposed model and the algorithm.

A. Data description

Fig. 5 shows the revised IEEE 123-bus system with eight damaged lines. There are thirteen automatic line switches, which can be used for system reconfiguration. There are two groups of repair crews for independent repairs. Each group of repair crew can be arranged to repair damaged lines via different paths. The repair time for one damaged line and the transportation time from the previous location are different. In this study, the transportation time is included in the repair time, and it is assumed that the repair time is satisfied as normal distributions. \( T \) in (22) shows the mean values (minutes) of the normal distributions. The element \( T_{ij}, i \neq j, i \in \{1, \cdots, 8\}, j \in \{1, \cdots, 8\} \) denotes the total period from the damaged line \( i \) to the damaged line \( j \) with the addition of the repair time for the damaged line \( j \). The element \( T_{ij}, i \in \{9\}, j \in \{1, \cdots, 8\} \) denotes the total period from the depot location to the damaged line \( j \) with the addition of the repair time for the damaged line \( j \). The element \( T_{ij}, i \in \{1, \cdots, 8\}, j \in \{9\} \) denotes the total period from the damaged line \( i \) to the depot location. The variance for each period is 6 minutes. Table I lists the damaged lines, and Table II lists the dispatchable lines.

![Image](https://example.com/image)

**TABLE I DAMAGED LINES**

<table>
<thead>
<tr>
<th>Label</th>
<th>Lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>F1</td>
<td>18-116</td>
</tr>
<tr>
<td>F2</td>
<td>42-44</td>
</tr>
<tr>
<td>F3</td>
<td>35-36</td>
</tr>
<tr>
<td>F4</td>
<td>64-65</td>
</tr>
</tbody>
</table>

**TABLE II DISPATCHABLE LINES**

<table>
<thead>
<tr>
<th>No.</th>
<th>Lines</th>
<th>No.</th>
<th>Lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>16-96</td>
<td>8</td>
<td>51-108</td>
</tr>
<tr>
<td>2</td>
<td>92-120</td>
<td>9</td>
<td>115-116</td>
</tr>
<tr>
<td>3</td>
<td>56-76</td>
<td>10</td>
<td>71-85</td>
</tr>
<tr>
<td>4</td>
<td>39-57</td>
<td>11</td>
<td>54-57</td>
</tr>
<tr>
<td>5</td>
<td>38-43</td>
<td>12</td>
<td>91-93</td>
</tr>
<tr>
<td>6</td>
<td>30-42</td>
<td>13</td>
<td>67-117</td>
</tr>
<tr>
<td>7</td>
<td>46-65</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

B. Estimated values of \( Q \) values

For the proposed model of uncertainty-inflicted event-driven repairs and reconfiguration, the \( Q \) values for semi-Markov states are important to transform the original recursive model with uncertainty to an event-driven deterministic optimization.
model. The $Q$ values for semi-Markov states are estimated by means of off-line learning and optimization. Fig. 6(a), (b), (c), (d), (e), and (f) show $Q$ values of different semi-Markov states with different load levels over the time horizon. It is observed that the $Q$ value for each semi-Markov state is converged to a constant after 15000 iterations. With the converged $Q$ values, i.e., the values of $Q'(S_t, \cdot)$, the optimization model (12) is transformed into an event-driven deterministic optimization model, which can be optimized easily. In each time period, the load levels are different, and in consequence the converged $Q$ values for semi-Markov states in different load levels are also varying. Fig. 7 shows the converged $Q$ values of the semi-Markov states in different time period. Based on those converged $Q$ values, the system operators can make sequential decisions according to event-driven repairs and reconfiguration. The following section will introduce how to make event-driven decisions in consideration of uncertain events over time horizon.

### C. Uncertainty-inflicted event-driven repairs and reconfiguration

Termination of one repair is considered as the start of another event-driven repair/reconfiguration. Because the period of repair is uncertain, the decision point is uncertain and is dependent on the termination of previous repairs. It is necessary to translate the findings of this study into practical applications. Fig. 8 shows three scenarios to illustrate the uncertainty-inflicted event-driven decision making process.

At the beginning, crew 1 and crew 2 are located at depots, and this can be considered as the same event when making decision from the depots. In consequence, the repair strategy (i.e., crew 1 needs to repair $F_3$ and crew 2 needs to repair $F_8$) and the reconfiguration strategy (i.e., the 8th, 12th, and 13th dispatchable lines are connected) are the same for the three cases. After making decision at the initial time, uncertain

Fig. 8. Uncertainty-inflicted event-driven repairs and reconfiguration for case I (a), case II (b), and case III (c).
periods of repairs will lead to different ‘events’. Different events cause different decision-making actions.

For the case I in Fig. 8 (a), the repair on $F_3$ implemented by crew 2 is finished at 56.9 mins, but the repair on $F_4$ implemented by crew 1 is not finished at this time. At this time point, the event-driven strategy is that the crew 2 starts to repair $F_7$ and the 3rd, 12th, and 13th dispatchable lines need to be connected. Then, the repair on $F_1$ implemented by crew 1 is finished at 95.6 mins and the repair on $F_7$ implemented by crew 2 is not finished at this time, the event-driven strategy is that the crew 1 starts to repair $F_3$ and the 1st, 3rd, and 13th dispatchable lines need to be connected. All damaged lines are repaired by means of similar event-driven strategies dependent on uncertain time periods of repairs implemented by the crews in the real world.

For the case II in Fig. 8 (b), the repair on $F_4$ implemented by crew 1 is finished at 46.8 mins, but the repair on $F_3$ implemented by crew 2 is not finished at this time. At this time point, the event-driven strategy is that the crew 1 starts to repair $F_7$ and the 2rd, 12th, and 13th dispatchable lines need to be connected. Then, the repair on $F_3$ implemented by crew 2 is finished at 51.6 mins and the repair on $F_7$ implemented by crew 1 is not finished at this time, the event-driven strategy is that the crew 2 starts to repair $F_1$ and the 2st, 12rd, and 13th dispatchable lines need to be connected. All damaged lines are repaired by means of similar event-driven strategies dependent on uncertain time periods of repairs.

For the case III in Fig. 8 (c), the repair on $F_3$ implemented by crew 2 is finished at 70.2 mins, but the repair on $F_4$ implemented by crew 1 is not finished at this time. At this time point, the event-driven strategy is that the crew 2 starts to repair $F_7$ and the 11rd, 12th, and 13th dispatchable lines need to be connected. Then, the repair on $F_3$ implemented by crew 2 is finished at 142.7 mins and the repair on $F_7$ implemented by crew 1 is still not finished at this time, the event-driven strategy is that the crew 2 starts to repair $F_1$ and the 2st, 12rd, and 13th dispatchable lines need to be connected. All damaged lines are repaired by means of similar event-driven strategies dependent on uncertain time periods of repairs.

Based on the above three cases, the repair decisions are made based on the ‘actual event’. In the real world, ‘actual event’ depends on the uncertain periods of the repairs. Take the case II as an example. The ‘actual event’ can be interpreted as that the repair on $F_4$ implemented by crew 1 is finished at 46.8 mins and the repair on $F_3$ implemented by crew 2 is not finished at 46.8 mins. For this uncertainty-inflicted ‘actual event’, the event-driven strategy is that the crew 1 starts to repair $F_7$ and the 2rd, 12th, and 13th dispatchable lines are connected. Therefore, the strategies in practice are event-driven with full consideration of the uncertain decision points due to uncertain events.

D. Impacts of Q-learning parameter $\lambda$ on converged Q Values

When updating the estimated Q values, the parameter $\lambda$ in the (16) has an impact on the convergence. Fig. 9 shows the curve of the Q values of four semi-Markov states with different $\lambda$. When fixing the value of $exp(-\lambda)$ at 0.95 and 0.85, the converged Q values approximately equal. With a smaller fixed value of $exp(-\lambda)$, e.g., 0.75, 0.65, and 0.55, the converged Q values have larger deviations but have faster convergence rates. The red lines represent the proposed dynamic $\lambda$ for the four semi-Markov states. It is observed that the proposed approach with the dynamic $\lambda$ has the fast convergence rate and smaller deviations.

In the simulation, the dynamic $\lambda$ is defined as the mean value of slopes of Q value curves. To simplify the calculation, it is assumed that the dynamic $\lambda$ is updated after a given iteration and the updated value is the mean value of slopes of
Based on the estimated values from the offline calculation can be used to accelerate the computational speed.

In addition, parallelism can be used to improve the accuracy of the model. The key idea of the constraints (10) is a time-consuming task, it is acceptable due to offline calculation. In addition, parallelism can be used to improve the accuracy of the model but also increase the solution time. Because this study focuses on the uncertainty-inflicted event-driven process, more accurate approximations of the constraints (10) are not investigated. In addition, the current approximation for the constraints (10) is used in some existing studies, also indicating the acceptable accuracy.

2) Computation time: The whole process includes offline Q learning and online decision-making. In our case study, the average calculation time of offline Q learning takes 110 hours. Although Q learning is a time-consuming task, it is acceptable due to offline calculation. In addition, parallel calculation can be used to accelerate the computational speed. Based on the estimated values from the offline Q learning, the online decision-making problem can be transformed into an event-driven deterministic optimization model, i.e., a one-step deterministic optimization model listed in (14). The calculation time for this one-step deterministic optimization model in the case study is 5 seconds on average, and this is acceptable for uncertainty-inflicted event-driven repair/reconfiguration action.

3) Application Scope: As described in the paper, the proposed model can be directly used for radial distribution systems. We would like to clarify that the concept and the framework of the uncertainty-inflicted event-driven process can be used for different power systems, e.g., non-radial distribution systems and transmission systems. The difference between different systems on the detailed model is the operational constraints, i.e., (6)-(12). In addition, more reinforcement learning approaches, e.g., deep deterministic policy gradient (DDPG), advantage actor critic (A2C), asynchronous advantage actor-critic (A3C), and soft actor-critic (SAC), can be used to solve the proposed model. With deep reinforcement learning approaches, the action for one semi-Markov state and the corresponding reward after the action can be generated via two deep neural networks. Solving the proposed model with deep reinforcement learning approaches is a promising point in the future.

VI. CONCLUSION

In consideration of sequential and uncertain decision point caused by uncertain repair time, this paper investigated semi-Markov decision process-based resilient recovery with uncertainty-inflicted event-driven repairs. A uncertainty-inflicted event-driven process is employed to represent the sequential repair/reconfiguration in consideration of uncertain repair time. Sequential repair implemented by different repair crews are modeled as semi-Markov states, with which the whole process is established as a semi-Markov decision process-based optimization model, which is an event-driven recursive model. Q-learning is employed to solve the proposed model, and the dynamic learning rates based on the slopes Q value curves for semi-Markov states are used to improve the convergence.

Based on the simulations, we have the following conclusions. (1) The semi-Markov decision process-based recursive optimization model can well represent the uncertainty-inflicted and sequential event-driven repairs. (2) The Q-learning approach with the dynamic learning rates based on the slopes Q value curves for semi-Markov states has faster convergence. (3) With the convergent estimations for semi-Markov states, the original event-driven recursive model with uncertainty can be transformed into an event-driven deterministic optimization model, i.e., a one-step deterministic optimization model.

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